# Characterizing immune correlates of protection in vaccine efficacy trials with stochastic-interventional causal effects

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Identifying immune correlates of vaccination for HIV-1 and COVID-19

#### The fights against HIV-1 and COVID-19

- The HIV-1 epidemic:
  - 1.5 million new infections occurring annually worldwide;
  - new infections outpace patients starting antiretroviral therapy;
  - HIV Vaccine Trials Network's (HVTN) 505 trial evaluated a novel antibody boost vaccine (Hammer et al. 2013).
- The COVID-19 epi pan endemic (Antia and Halloran 2021):
  - 270 331 619 643 770 million total cases detected globally;
  - new variants emerging, with continued formulation of targeted vaccines and annual roll-outs expected;
  - COVID-19 Prevention Network's (CoVPN) COVE trial focused on Moderna's (mRNA-1273) vaccine (Baden et al. 2021).

#### **Evaluating vaccines for HIV-1 and COVID-19**

- 505: How would HIV-1 infection risk have differed had the boost vaccine modulated antibody responses differently?
- COVE: How would COVID-19 disease risk have differed for alternative vaccine-induced immunogenic response profiles?
- Question: How can [HIV-1, COVID-19] vaccines be improved through the modulation of immunogenic response profiles?

# Why measure and analyze immune correlates?

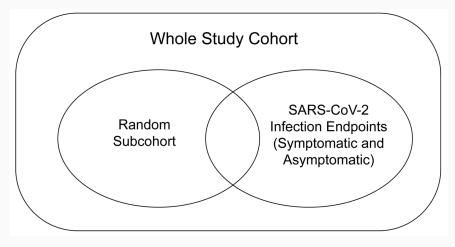
- Two, interrelated goals of immune correlates analyses are to
  - identify/validate possible *surrogate endpoints* (Prentice 1989);
  - understand/delineate *protective mechanisms* of vaccines.
- If an immune correlate is established to reliably predict VE, subsequent efficacy trials may use it as a primary endpoint.
- This may accelerate the approval of
  - existing vaccines in different populations (e.g., in children);
  - new vaccines within the same class (e.g., bivalent mRNA);
  - inform the development of "next-generation" vaccines.

# Measuring correlates: Two-phase designs

- Often, use case-cohort design (Prentice 1986), a special case of two-phase sampling (Breslow et al. 2003).
- Phase 1: measure baseline, vaccination, endpoint on everyone.
- Phase 2: given baseline, vaccine, endpoint, select members of immune response subcohort with (possibly known) probability.
  - 505: phase-two sample with 100% of HIV-1 cases and matching of non-cases (n = 189 per Janes et al. 2017).
  - COVE: stratified random subcohort ( $n \approx 1600$ ) and all SARS-CoV-2 infection and COVID-19 disease endpoints.

#### A simple two-phase design: Case-cohort

Assaying >30k samples is expensive, statistically unnecessary.



Case-cohort design, per Prentice (1986), as applied to COVE.

#### Two-phase sampling masks the complete data structure

- Complete (unobserved) data  $X = (L, A, S, Y) \sim P_0^X \in \mathcal{M}$ :
  - L (baseline covariates): sex, age, BMI, behavioral HIV risk,
  - A (treatment): randomized assignment to vaccine/placebo,
  - S (exposure): immune response profile for relevant markers,
  - Y (outcome of interest): infection status at trial's end.
- Observed data  $O = (V, B, BX) = (L, A, B, BS, Y) \sim P_0 \in \mathcal{M}$ .
  - $V \equiv (L, Y)$  are used in defining *outcome-dependent* two-phase sampling mechanism  $g_{0,B} := \mathbb{P}(B = 1 \mid V)$ .
  - $B \in \{0,1\}$  is an indicator of inclusion in the phase-two sample.
  - $g_{0,B} := \mathbb{P}(B=1 \mid Y, L)$  must be *known by design* or estimated.

Causal effects for quantitative exposures

#### Static interventions aren't enough

 Describe the manner in which X is hypothetically generated by a nonparametric structural equation model (Pearl 2009):

$$L = f_L(U_L); A \sim \text{Bern}(0.5); S = f_S(A, L, U_S); Y = f_Y(S, A, L, U_Y)$$

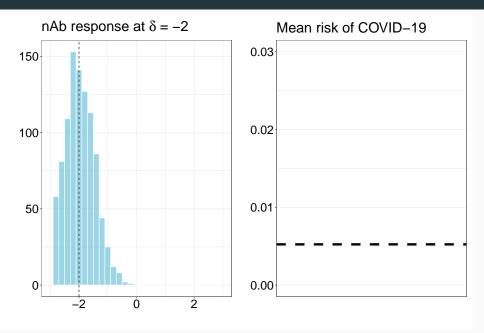
- Utility: Implies a model for the distribution of counterfactual RVs induced by interventions on the system under study.
- A *static* intervention replaces  $f_S$  with a specific value s in its conditional support, i.e.,  $S \mid L$ .
- This requires specifying a priori a particular value of exposure under which to evaluate the outcome — but what value?

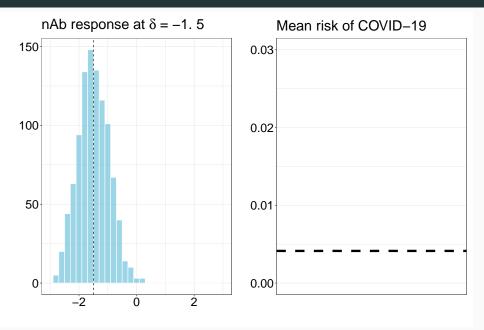
# Controlled vaccine efficacy (CVE)

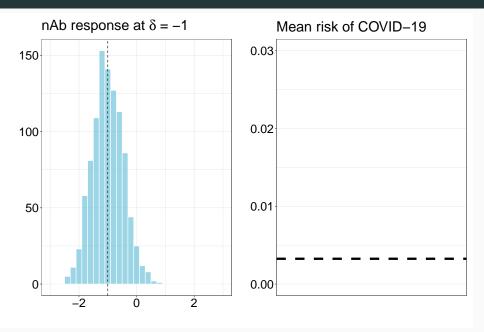
- For a hypothetical value  $s \in \mathcal{S}$ , the controlled direct effect (CDE) quantifies the effect of A on Y while fixing S = s.
- The hypothetical value S = s must be chosen carefully to be scientifically informative and to avoid positivity violations.
- For two hypothetical values  $s_0, s_1 \in \mathcal{S}$ , Controlled Vaccine Efficacy (CVE) (Gilbert et al. 2022) is

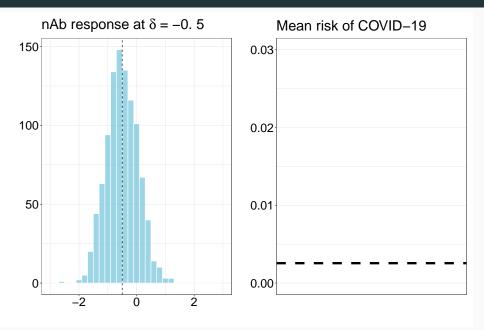
$$\mathsf{CVE}(s_0, s_1) = 1 - \frac{\mathbb{E}[\mathbb{P}(Y = 1 \mid S = s_1, A = 1, L = l)]}{\mathbb{E}[\mathbb{P}(Y = 1 \mid S = s_0, A = 0, L = l)]},$$

which contrasts counterfactual risk for vaccine and  $S=s_1$  vs. placebo and  $S=s_0$ , where  $s_0=0$  by construction.









#### Stochastic interventions define the causal effects of shifts

- Stochastic interventions modify the value *S* would naturally assume by *shifting* the natural exposure distribution.
- Díaz and van der Laan (2012; 2018)'s shift interventions<sup>1</sup>

$$d(s, l) = \begin{cases} s + \delta, & s + \delta < u(l) & \text{(if plausible)} \\ s, & s + \delta \ge u(l) & \text{(otherwise)} \end{cases}$$

• Our estimand is  $\psi_{0,\delta} \coloneqq \mathbb{E}_{P_{\delta,0}}\{Y^{d(S,L)}\}$ , which is identified by

$$\psi_{0,\delta} = \int_{\mathcal{L}} \int_{\mathcal{S}} \mathbb{E}_{P_0} \{ Y \mid S = d(s, l), L = l \}$$
$$g_{0,S}(s \mid L = l) q_{0,L}(l) d\mu(s) d\nu(l)$$

<sup>&</sup>lt;sup>1</sup>Haneuse and Rotnitzky (2013) introduced modified treatment policies.

# Causal interpretation of statistical target parameter

# Assumption 1: Stable unit treatment value (SUTVA)

- $Y_i^{d(s_i,l_i)}$  does not depend on  $d(s_j,l_j)$  for  $i=1,\ldots,n$  and  $j \neq i$ , or lack of interference (Cox 1958, Rubin 1974)
- $Y^{d(s,l)} = Y$  in the event S = d(s,l), for i = 1, ..., n

#### Assumption 2: No unmeasured confounding

$$Y^{d(s,l)} \perp S \mid L = l$$
, for  $i = 1, \ldots, n$ 

# Assumption 3: Structural positivity

 $s \in \mathcal{S} \implies d(s, l) \in \mathcal{S}$  for all  $l \in \mathcal{L}$ , where  $\mathcal{S}$  denotes the support of S conditional on L = l for all i = 1, ..., n

#### Interpreting the causal effects of shift interventions

- Consider a data structure:  $(Y_s, s \in S)$ .
- Let  $Y_s = \beta_0 + \beta_1 s + \epsilon_s$ , with error  $\epsilon_s \sim N(0, \sigma_s^2) \ \forall \ s \in S$ .
- For the counterfactual outcomes  $(Y_{s'+\delta}, Y_{s'})$ , their difference  $Y_{s'+\delta} Y_{s'}$  may be expressed (for some  $s' \in \mathcal{S}$ )

$$\mathbb{E}Y_{s'+\delta} - \mathbb{E}Y_{s'} = [\beta_0 + \beta_1(s'+\delta) + \mathbb{E}\epsilon_{s'+\delta}] - [\beta_0 + \beta_1s' + \mathbb{E}\epsilon_{s'}]$$

$$= \beta_0 - \beta_0 + \beta_1s' - \beta_1s' + \beta_1\delta$$

$$= \beta_1\delta$$

• A unit shift for  $s' \in S$  (i.e., for  $\delta = 1$ ) causes a counterfactual difference in Y of magnitude  $\beta_1$  in this simple schematic.

# Stochastic-interventional vaccine efficacy (SVE)

Statistical parameter for vaccine efficacy (VE) estimands:

$$\begin{aligned} \mathsf{SVE}(\delta) &= 1 - \frac{\mathbb{E}[\mathbb{P}(Y = 1 \mid S = d(s, l), A = 1, L = l)]}{\mathbb{P}(Y = 1 \mid A = 0)} \\ &= 1 - \frac{\psi_{0, \delta}}{\mathbb{P}(Y = 1 \mid A = 0)} \end{aligned}$$

- $\mathbb{P}(Y=1 \mid A=0)$ : counterfactual risk in the placebo arm i.e., under randomization,  $\mathbb{P}(Y=1 \mid A=0) \equiv \mathbb{P}(Y(0)=1)$ .
- Summarizes VE via stochastic interventions across  $\delta$ , per the CoVPN immune correlates SAP<sup>2</sup> (Gilbert et al. 2021a;b).

<sup>&</sup>lt;sup>2</sup>SAP published at https://doi.org/10.6084/m9.figshare.13198595.

Efficient estimation in two-phase designs

#### Estimation of the counterfactual mean $\psi_{0,\delta}$

A RAL estimator  $\psi_{n,\delta}$  of  $\psi_{0,\delta} := \Psi(P_0)$  is efficient if and only if

$$\psi_{n,\delta} - \psi_{0,\delta} = \frac{1}{n} \sum_{i=1}^{n} D^{*}(P_0)(O_i) + o_P(n^{-1/2}) ,$$

where  $D^*(P)$  is the efficient influence function (EIF) of  $\psi_{0,\delta}$  with respect to the nonparametric model  $\mathcal{M}$  at a distribution  $P \in \mathcal{M}$ .

The EIF of  $\psi_{0,\delta}$  is indexed by two key *nuisance parameters* 

$$\overline{Q}_{Y}(S,L) := \mathbb{E}_{P}(Y \mid S, A = 1, L)$$
 outcome mechanism  $g_{S}(S \mid L) := f_{P}(S \mid A = 1, L)$  generalized propensity score

#### Flexible, efficient, doubly robust estimation

• The efficient influence function of  $\psi_{0,\delta}$  with respect to  $\mathcal M$  is

$$D_F^*(P_0)(o) = \frac{g_{0,S}(d^{-1}(s,l)|l)}{g_{0,S}(s|l)}(y - \overline{Q}_{0,Y}(s,l)) + \overline{Q}_{0,Y}(d(s,l),l) - \psi_{0,\delta}.$$

The one-step bias-corrected estimator:

$$\psi_n^+ = \frac{1}{n} \sum_{i=1}^n \overline{Q}_{n,Y}(d(S_i, L_i), L_i) + D_{F,n}^*(O_i) .$$

■ The TML estimator updates initial estimates of  $\overline{Q}_{n,Y}$  to  $\overline{Q}_{n,Y}^*$  via a tilting procedure that sets  $\mathbb{E}_P D_{F,n}^*(P_0)(O) \approx 0$ :

$$\psi_n^{\star} = \frac{1}{n} \sum_{i=1}^n \overline{Q}_{n,Y}^{\star}(d(S_i, L_i), L_i) .$$

"Double robust" – flexible modeling of nuisance parameters.

# Augmented estimators for two-phase sampling designs

 Rose and van der Laan (2011) suggested inverse probability of censoring weighted (IPCW) loss functions:

$$\mathcal{L}(P_0^X)(O) = \frac{B}{g_{0,B}(Y,L)} \mathcal{L}(P_0^X)(X)$$

- When the sampling mechanism  $g_{0,B}(Y,L)$  is known by design, this procedure yields a reasonably reliable estimator.
- When data-adaptive regression is warranted that is, when  $g_{0,B}(Y,L)$  is not known by design<sup>3</sup>— this is inefficient.

<sup>&</sup>lt;sup>3</sup>Sampling of non-cases in HVTN 505 used matching (Janes et al. 2017).

# Efficiency and multiple robustness (Hejazi et al. 2021)

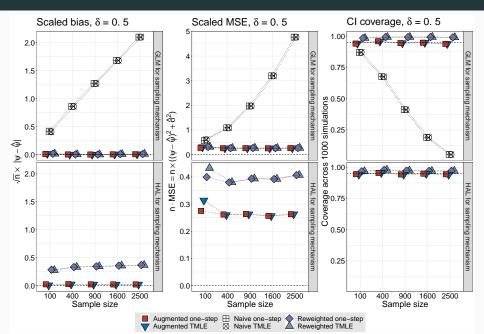
• Then, the IPCW augmentation must be applied to the EIF<sup>4</sup>:

$$D^{*}(P_{0}^{X})(o) = \frac{b}{g_{0,B}(y,l)} D_{F}^{*}(P_{0}^{X})(x) - \left(1 - \frac{b}{g_{0,B}(y,l)}\right)$$
$$\mathbb{E}(D_{F}^{*}(P_{0}^{X})(x) \mid B = 1, Y = y, L = l).$$

- Expresses observed data EIF  $D^*(P_0^X)(o)$  via complete data EIF  $D_F^*(P_0^X)(x)$ ; inclusion of second term improves efficiency.
- An emergent robustness property one each of  $g_{0,S}(S \mid L)$ ,  $\overline{Q}_{0,Y}(S,L)$  and  $g_{0,B}(Y,L)$ ,  $\mathbb{E}(D_F^*(P_0^X)(x) \mid B=1,Y,L)$ .
- Our txshift R package implements our estimators of  $\psi_{0,\delta}.$

<sup>&</sup>lt;sup>4</sup>Robins et al. (1994) explored a similar correction for related sampling designs.

#### Comparing reweighted and augmented estimators



Predicting and bridging vaccine efficacy

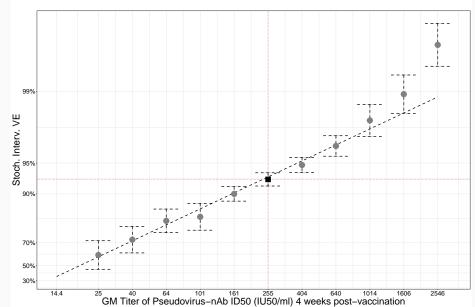
#### SVE prediction of HIV-1 risk in the HVTN 505 trial

TML estimates of mean counterfactual HIV-1 infection risk under shifted CD8+ polyfunctionality with pointwise confidence intervals and summarization via working marginal structural model (\$\hat{\beta}\_{TMI,F} = -0.013) 0.10 0.08 ----Risk of HIV-1 infection 0.00 90.0 0.02 0.00 -2 Posited change in standardized CD8+ polyfunctionality (sd units)

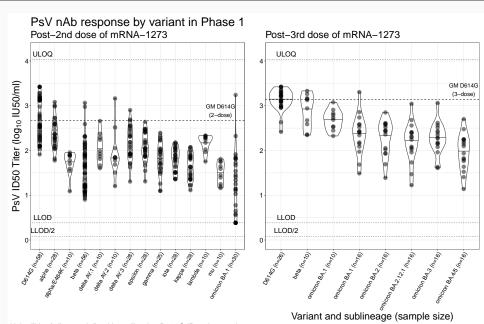
HIV-1 risk change across CD8+ score (txshift R package).

#### SVE prediction of mRNA-1273 VE in the CoVPN COVE trial

Stoch. Interv. VE vs. COVID-19 (4 weeks post-vaccination with 100 days follow-up)



# Pooled phase 1 studies: PsV nAb responses across variants



#### SVE bridging of mRNA-1273 VE (Hejazi et al. 2023)

Stoch. Interv. VE vs. COVID-19 (4 weeks post-vaccination with 100 days follow-up) After 2 doses of mRNA-1273 \_ J.\_ 99% Stoch. Interv. VE 70% 50% 30% 10% GM Titer of Pseudovirus-nAb ID50 (IU50/ml) 4 weeks post-vaccination SARS-CoV-2 variant delta lambda

#### The Big Picture

- Flexible stochastic interventions help to formulate novel modified treatment policies (based on "natural" treatment conditions).
- Modified treatment policies address causal questions about realistic manipulations of quantitative intervention variables.
- Large-scale vaccine trials routinely use two-phase designs but need to adjust (carefully!) for resultant sampling bias.
- Efficient estimators with double/multiple robustness can safely answer such questions while incorporating machine learning.
- Open source software for such statistical analyses is critical for the methods to have any impact on real-world studies.

# Thank you!

Thanks for listening. Any questions?

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https://doi.org/10.1111/biom.13375

Hejazi et al. (2023) to appear in IJID

Appendix

# Immune correlates of protection (Plotkin and Gilbert 2012)

- Correlate of Protection (CoP): immune marker statistically predictive of vaccine efficacy, not necessarily mechanistic.
- Mechanistic CoP (mCoP): immune marker that is causally and mechanistically responsible for protection.
- Nonmechanistic CoP (nCoP): immune marker that is predictive but not a causal agent of protection.
- A CoP is a candidate surrogate endpoint (Prentice 1989) primary endpoint in future trials if reliably predictive.

# Literature: Díaz and van der Laan (2012; 2018)

- Proposal: Evaluate outcome under an altered intervention distribution e.g.,  $P_{\delta}(g_{0,S})(S=s\mid L)=g_{0,S}(s-\delta(L)\mid L)$ .
- Identification conditions for a statistical parameter of the counterfactual outcome  $\psi_{0,\delta}$  under such an intervention.
- Show that the causal quantity of interest  $\mathbb{E}_{P_0^{\delta}}\{Y_{d(S,L)}\}$  is identified by a functional of the distribution of O, i.e.,

$$\psi_{0,\delta} = \int_{\mathcal{L}} \int_{\mathcal{S}} \mathbb{E}_{P_0} \{ Y \mid S = d(s, l), L = l \}$$
$$g_{0,S}(s \mid L = l) \cdot q_{0,L}(l) d\mu(s) d\nu(l)$$

# Literature: Haneuse and Rotnitzky (2013)

- Proposal: Characterization of stochastic interventions as modified treatment policies (MTPs).
- Assumption of piecewise smooth invertibility allows for the post-intervention distribution of any MTP to be recovered:

$$g_{0,S}(s \mid l; \delta) = \sum_{j=1}^{J(l)} \mathbb{I}_{\delta,j}\{h_j(s, l), l\}g_{0,S}\{h_j(s, l) \mid l\}h_j'(s, l)$$

 MTPs account for the natural value of exposure S yet may be interpreted as imposing an altered intervention mechanism.

#### Slope in a semiparametric model

• Consider the stochastic intervention  $g_{\delta}(\cdot \mid L)$ :

$$\mathbb{E}Y_{g_{\delta}} = \int_{L} \int_{s} \mathbb{E}(Y \mid S = s, L)g(s - \delta \mid L)dsdP_{0}(L)$$
$$= \int_{L} \int_{z} \mathbb{E}(Y \mid S = z + \delta, L)g(z \mid L)dzdP_{0}(L),$$

defining the change of variable  $z = s - \delta$ .

• For a semiparametric model,  $\mathbb{E}(Y \mid S = z, L) = \beta z + \theta(L)$ :

$$\mathbb{E}Y_{g_{\delta}} - \mathbb{E}Y = \int_{L} \int_{z} \left[ \mathbb{E}(Y \mid S = z + \delta, L) - \mathbb{E}(Y \mid S = z, L) \right]$$
$$g(z \mid L) dz dP_{0}(L)$$
$$= \left[ \beta(z + \delta) + \theta(L) \right] - \left[ \beta z + \theta(L) \right]$$
$$= \beta \delta$$

# Flexible conditional density estimation of $g_{0,S}$

Díaz and van der Laan (2011)'s conditional density estimator:

$$g_{n,\alpha}(s \mid L) = \frac{\mathbb{P}(s \in [\alpha_{t-1}, \alpha_t) \mid L)}{\alpha_t - \alpha_{t-1}}.$$

- Re-expressed as hazard regressions in repeated measures data.
- Tuning parameter  $t \approx \text{bandwidth in kernel density estimation}$ .
- When càdlàg (RCLL) with finite sectional variation, we have

$$\operatorname{logit}\{\mathbb{P}(s \in [\alpha_{t-1}, \alpha_t) \mid L)\} = \beta_0 + \sum_{w \subset \{1, \dots, d\}} \sum_{i=1}^n \beta_{w,i} \phi_{w,i},$$

for appropriate basis functions  $\{\phi_{w,i}\}_{i=1}^n$  (Gill et al. 1995).

# Flexible conditional density estimation of $g_{0,S}$

- Utilizing a particular basis construction for  $\phi_w$ , van der Laan (2017)'s HAL estimator achieves  $n^{-1/4}$  convergence rate<sup>5</sup>.
- Loss-based cross-validation allows selection of a suitable HAL estimator, which has only the  $\ell_1$  regularization term  $\lambda$ :

$$\beta_{n,\lambda} = \mathop{\arg\min}_{\beta: |\beta_0| + \sum_{w \subset \{1, \dots, d\}} \sum_{i=1}^n |\beta_{w,i}| < \lambda} P_n \mathcal{L}(g_{\beta,\lambda,S}),$$

where  $\mathcal{L}(\cdot)$  is an appropriate loss function, giving  $\{\lambda_n, \beta_n\}$ .

- We denote by  $g_{n,\lambda,S} := g_{\beta_{n,\lambda},S}$ , the HAL estimate of  $g_{0,S}$ .
- Our haldensify R package implements our estimator of  $g_{0,S}$ .

 $<sup>^6</sup>$ Similar rates can be achieved via *local* (vs. global) smoothness assumptions on  $g_{n,S}$  (see, e.g., Robins et al. 2008, Mukherjee et al. 2017, Liu et al. 2021).

#### A useful class of functions

Consider space of cadlag functions with finite variation norm.

**Def.** cadlag = *left-hand continuous* with *right-hand limits* 

**Variation norm** Let  $\theta_s(u) = \theta(u_s, 0_{s^c})$  be the section of  $\theta$  that sets the coordinates in s equal to zero.

The *variation norm* of  $\theta$  can be written:

$$|\theta|_{\nu} = \sum_{s \subset \{1,\ldots,d\}} \int |d\theta_s(u_s)|,$$

where  $x_s = (x(j) : j \in s)$  and the sum is over all subsets.

#### Sectional variation norm

We can represent the function  $\theta$  as

$$\theta(x) = \theta(0) + \sum_{s \subset \{1,...,d\}} \int \mathbb{I}(x_s \geq u_s) d\theta_s(u_s),$$

For discrete measures  $d\theta_s$  with support points  $\{u_{s,j}:j\}$  we get a linear combination of indicator basis functions:

$$\theta(x) = \theta(0) + \sum_{s \subset \{1,\dots,d\}} \sum_{j} \beta_{s,j} \theta_{u_{s,j}}(x),$$

where 
$$\beta_{s,j} = d\theta_s(u_{s,j})$$
,  $\theta_{u_{s,j}}(x) = \mathbb{I}(x_s \geq u_{s,j})$ , and

$$|\theta|_{\nu} = \theta(0) + \sum_{s \subset \{1, \dots, d\}} \sum_{i} |\beta_{s,j}|.$$

# Convergence rate for HAL estimators

We have, for  $\alpha(d) = 1/(d+1)$ ,

$$|\theta_{n,M} - \theta_{0,M}|_{P_0} = o_P(n^{-(1/4 + \alpha(d)/8)}).$$

Thus, if we select  $M > |\theta_0|_v$ , then

$$|\theta_{n,M} - \theta_0|_{P_0} = o_P(n^{-(1/4 + \alpha(d)/8)})$$
.

Due to oracle inequality for the cross-validation selector  $M_n$ ,

$$|\theta_{n,M_n} - \theta_0|_{P_0} = o_P(n^{-(1/4 + \alpha(d)/8)})$$
.

Improved convergence rate (Bibaut and van der Laan 2019):

$$|\theta_{n,M_n} - \theta_0|_{P_0} = o_P(n^{-1/3}\log(n)^{d/2})$$
.

#### Algorithm for TML estimation

- 1. Construct initial estimators  $g_{n,S}$  of  $g_{0,S}(S,L)$  and  $Q_{n,Y}$  of  $\overline{Q}_{0,Y}(S,L)$ , perhaps using data-adaptive regression techniques.
- 2. For each observation i, compute an estimate  $H_n(s_i, l_i)$  of the auxiliary covariate  $H_0(s_i, l_i)$ .
- 3. Estimate the parameter  $\epsilon$  in the logistic regression model

$$\operatorname{logit} \overline{Q}_{\epsilon,n,Y}(s,l) = \operatorname{logit} \overline{Q}_{n,Y}(s,l) + \epsilon H_n(s,l),$$

or an alternative regression model incorporating weights.

4. Compute TML estimator  $\Psi_n$  of the target parameter, defining the update  $\overline{Q}_{n,Y}^{\star}$  of the initial estimate  $\overline{Q}_{n,Y}$  to  $\overline{Q}_{\epsilon_n,n,Y}$ :

$$\Psi_n = \Psi(P_n^*) = \frac{1}{n} \sum_{i=1}^n \overline{Q}_{n,Y}^*(d(S_i, L_i), L_i).$$

#### Algorithm for IPCW-TML estimation

- 1. Using all observed units, estimate the sampling mechanism  $g_{0,B}(Y,L)$ , perhaps using data-adaptive regression methods.
- 2. Using only observed units in the phase-two sample B=1, construct initial estimators  $g_{n,S}(S,L)$  and  $\overline{Q}_{n,Y}(S,L)$ , weighting by the sampling mechanism estimate  $g_{n,B}(Y,L)$ .
- 3. With the approach described for the full data case, compute  $H_n(s_i, l_i)$ , and fluctuate submodel via logistic regression.
- 4. Compute IPCW-TML estimator  $\Psi_n$  of the target parameter, by solving the IPCW-augmented EIF estimating equation.
- 5. Iteratively update estimated sampling weights  $g_{n,B}(Y,L)$  and IPCW-augmented EIF, updating TMLE in each iteration.

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