Evaluating the causal impacts of vaccine-induced immune responses in two-phase vaccine efficacy trials

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The burden of HIV-1

- The HIV-1 epidemic — the facts:
  - now in its fourth decade,
  - 2.5 million new infections occurring annually worldwide,
  - new infections outpace patients starting antiretroviral therapy.
- *Most efficacious* preventive vaccine: $\sim$31% reduction rate.
- **Question**: To what extent can HIV-1 vaccines be improved by modulating immunogenic CD4+/CD8+ response profiles?

HVTN 505 trial examined new antibody boost vaccines

- HIV Vaccine Trials Network's (HVTN) 505 vaccine efficacy; randomized controlled trial, $n = 2504$ (Hammer et al. 2013).
- **Question:** How would HIV-1 infection risk in week 28 have changed had vaccine-induced immunogenic response differed?
- Immunogenic response profiles only available for second-phase sample of $n = 189$ (Janes et al. 2017) due to cost limitations.
- Two-phased sampling mechanism: 100% inclusion rate if HIV-1 positive in week 28; based on matching otherwise.

Two-phase sampling censors the complete data structure

- Complete (unobserved) data $X = (L, A, S, Y) \sim P_0^X \in \mathcal{M}^X$, as per the full HVTN 505 trial cohort (Hammer et al. 2013):
  - L (baseline covariates): sex, age, BMI, behavioral HIV risk,
  - A (treatment): vaccination status (randomized),
  - S (exposure): immune response profile for CD4+ and CD8+,
  - Y (outcome of interest): HIV-1 infection status at week 28.
- Observed data $O = (C, CX) = (L, C, CS, Y)$.
  - $C \in \{0, 1\}$ indicates inclusion in the second-phase sample.
  - Implicitly conditioning on the vaccine arm, i.e., $O = X \mid A = 1$.

NPSEM with static interventions

- Use a nonparametric structural equation model (NPSEM) to describe the generation of X (Pearl 2009), specifically

$$L = f_L(U_L); S = f_S(L, U_S); Y = f_Y(S, L, U_Y)$$

- Implies a model for the distribution of counterfactual random variables generated by interventions on the process.
- A *static intervention* replaces f_S with a specific value s in its conditional support $S \mid A = 1, L$.
- This requires specifying a particular value of the exposure under which to evaluate the outcome *a priori*.

NPSEM with stochastic interventions

- *Stochastic interventions* modify the value S would naturally assume by drawing from a modified exposure distribution.
- Consider the post-intervention value $S^\star \sim G^\star(\cdot \mid L)$; static interventions are a special case (degenerate distribution).
- Such an intervention generates a counterfactual random variable $Y_{G^\star} := f_Y(S^\star, L, U_Y)$, with distribution P_0^δ, .
- We aim to estimate $\psi_{0,\delta} := \mathbb{E}_{P_0^\delta}\{Y_{G^\star}\}$, the counterfactual mean under the post-intervention exposure distribution $G^\star$.

Stochastic interventions for the causal effects of shifts

- Díaz and van der Laan (2012; 2018)'s *stochastic* interventions

$$d(s, l) = \begin{cases} s + \delta, & s + \delta < u(l) \quad \text{(if plausible)} \\ s, & s + \delta \geq u(l) \quad \text{(otherwise)} \end{cases}$$

- Our estimand is $\psi_{0,d} := \mathbb{E}_{P_0^d}\{Y_{d(S,L)}\}$, mean of $Y_{d(S,L)}$.
- Statistical target parameter is $\Psi(P_0^X) = \mathbb{E}_{P_0^X}\overline{Q}(d(S, L), L)$, counterfactual mean of the *shifted* outcome mechanism.
- For HVTN 505, $\psi_{0,d}$ is the counterfactual risk of HIV-1 infection, had the observed value of the immune response been altered under the rule $d(S, L)$ defining $G^\star(\cdot \mid L)$.

From the causal to the statistical target parameter

Assumption 1: *Stable Unit Treatment Value (SUTVA)*

- $Y_i^{d(s_i,l_i)}$ *does not depend on* $d(s_j, l_j)$ *for* $i = 1, \ldots, n$ *and* $j \neq i$, *or lack of interference (Rubin 1978; 1980)*
- $Y_i^{d(s_i,l_i)} = Y_i$ *in the event* $S_i = d(s_i, l_i)$, *for* $i = 1, \ldots, n$

Assumption 2: *Ignorability*

$S_i \perp\!\!\!\perp Y_i^{d(s_i,l_i)} \mid L_i$, *for* $i = 1, \ldots, n$

Assumption 3: *Positivity*

$s_i \in \mathcal{S} \implies d(s_i, l_i) \in \mathcal{S}$ *for all* $l \in \mathcal{L}$, *where* $\mathcal{S}$ *denotes the support of* S *conditional on* $L = l_i$ *for all* $i = 1, \ldots n$

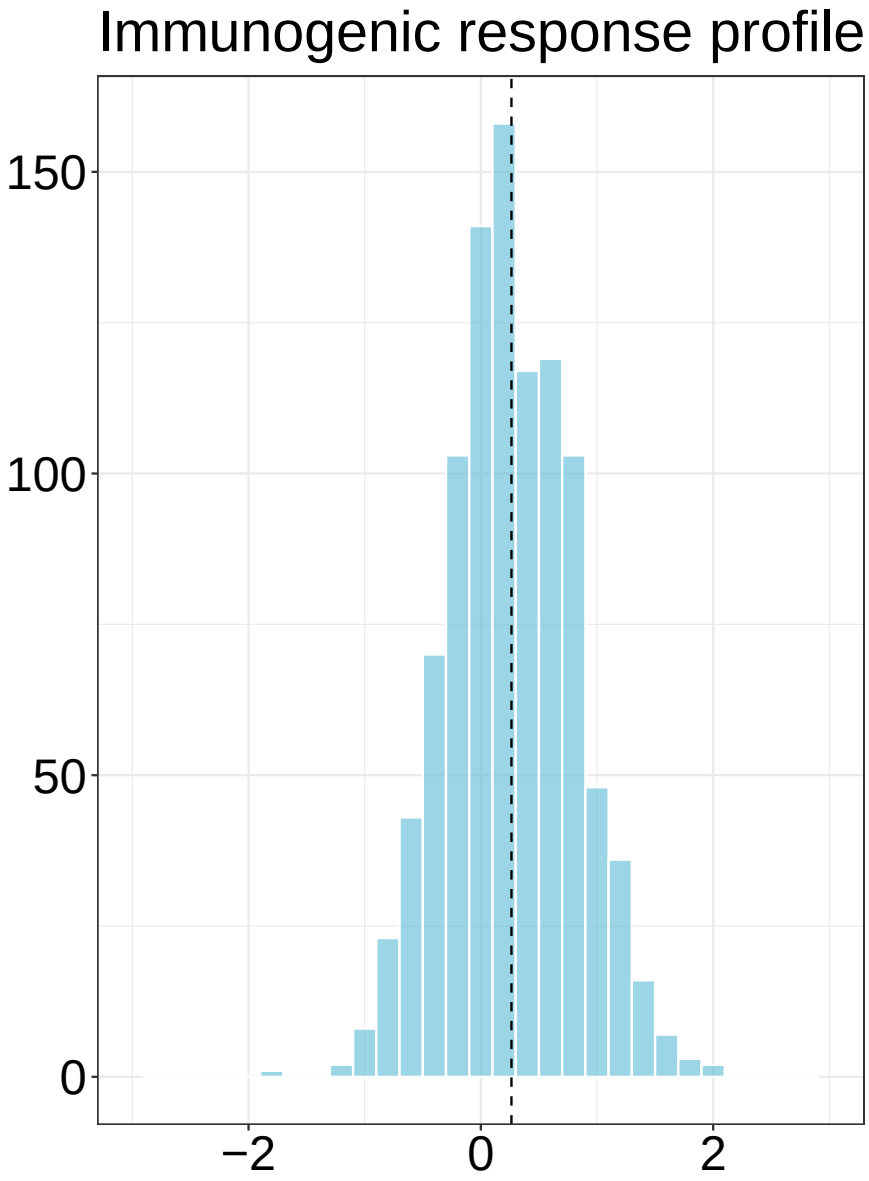
Literature: Díaz and van der Laan (2012)

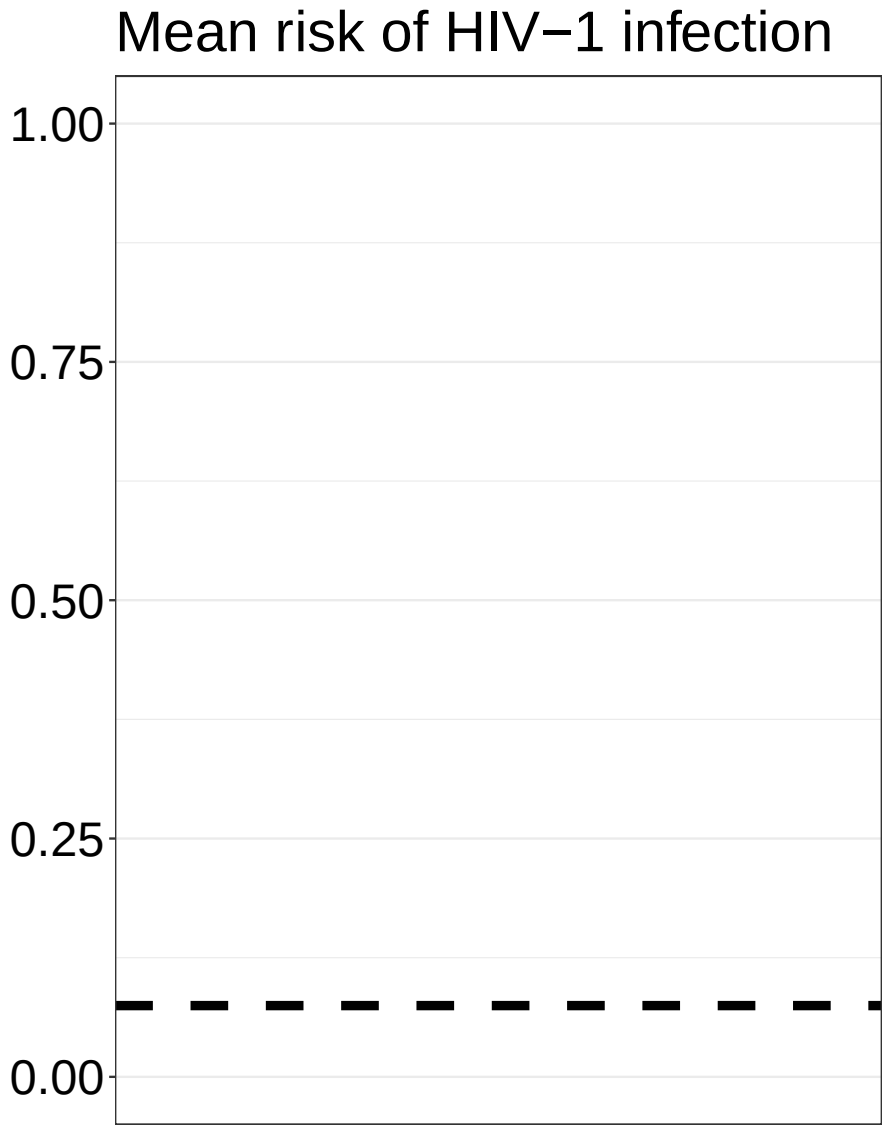
- *Proposal:* Evaluate outcome under an altered *intervention distribution* — e.g., $P_\delta(g_0)(S = s \mid L) = g_0(s - \delta(L) \mid L)$.
- Identification conditions for a statistical parameter of the counterfactual outcome $\psi_{0,d}$ under such an intervention.
- Show that the causal quantity of interest $\mathbb{E}_0\{Y_{d(S,L)}\}$ is identified by a functional of the distribution of X:

$$\psi_{0,d} = \int_{\mathcal{L}} \int_{\mathcal{S}} \mathbb{E}_{P_0^X}\{Y \mid S = d(s, l), L = l\} \cdot q_{0,S}^X(s \mid L = l) \cdot q_{0,L}^X(l) d\mu(s) d\nu(l)$$

- Provides a derivation based on the efficient influence function (EIF) with respect to the nonparametric model $\mathcal{M}$.

HIV-1 risk under shifted immunogenic responses





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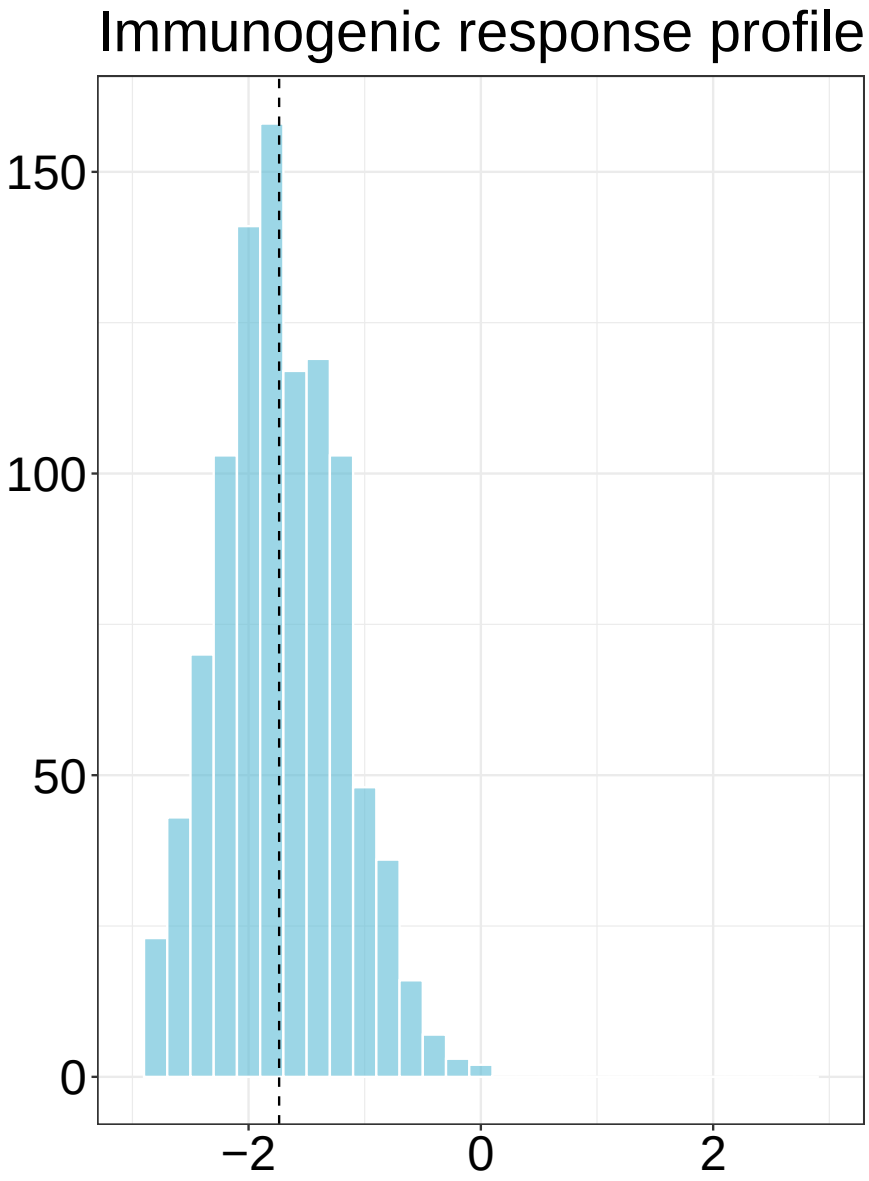

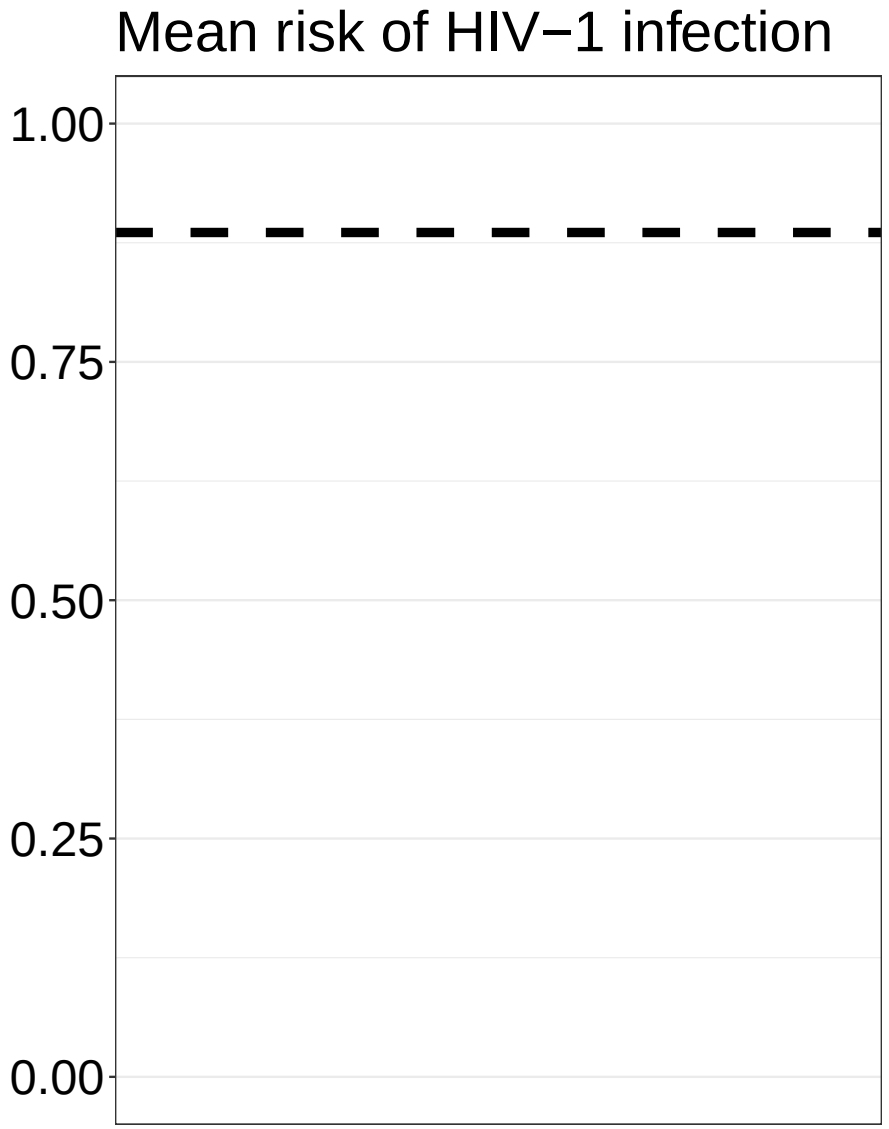

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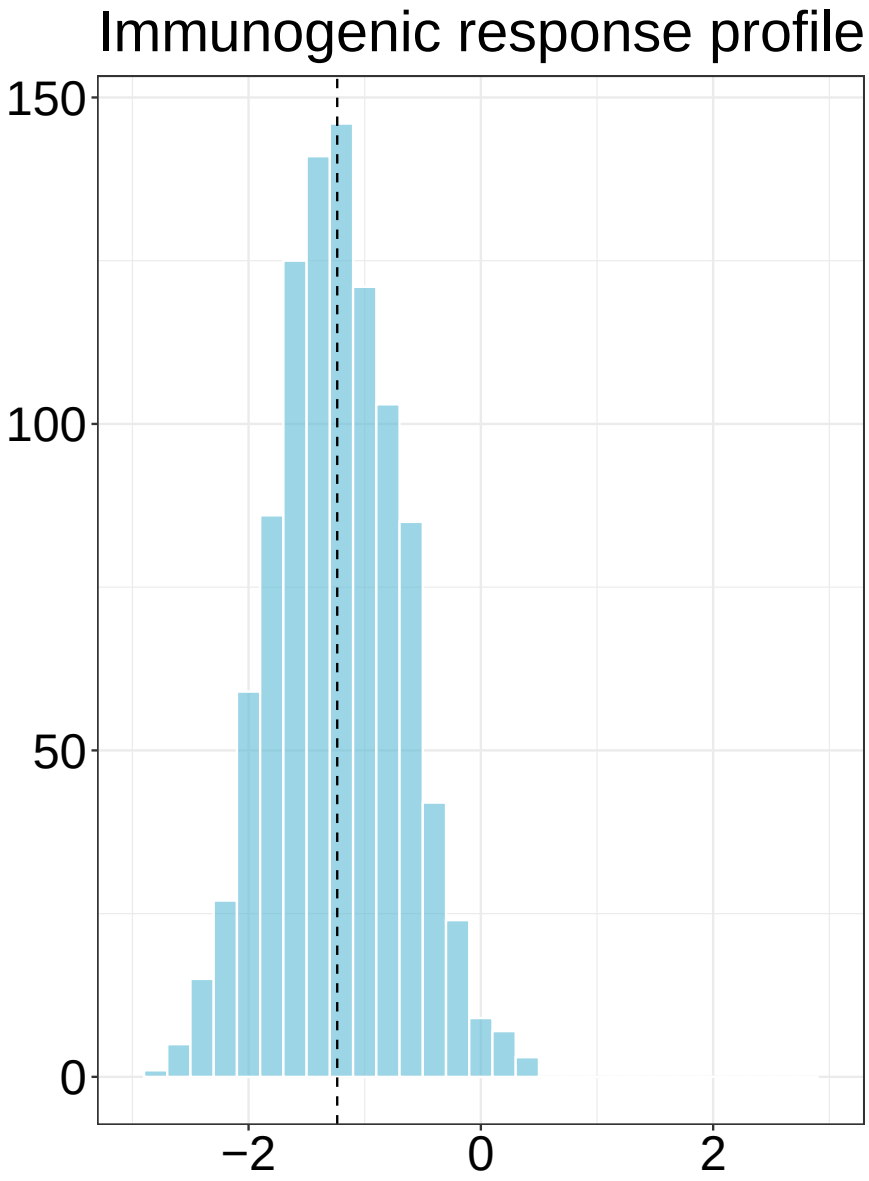

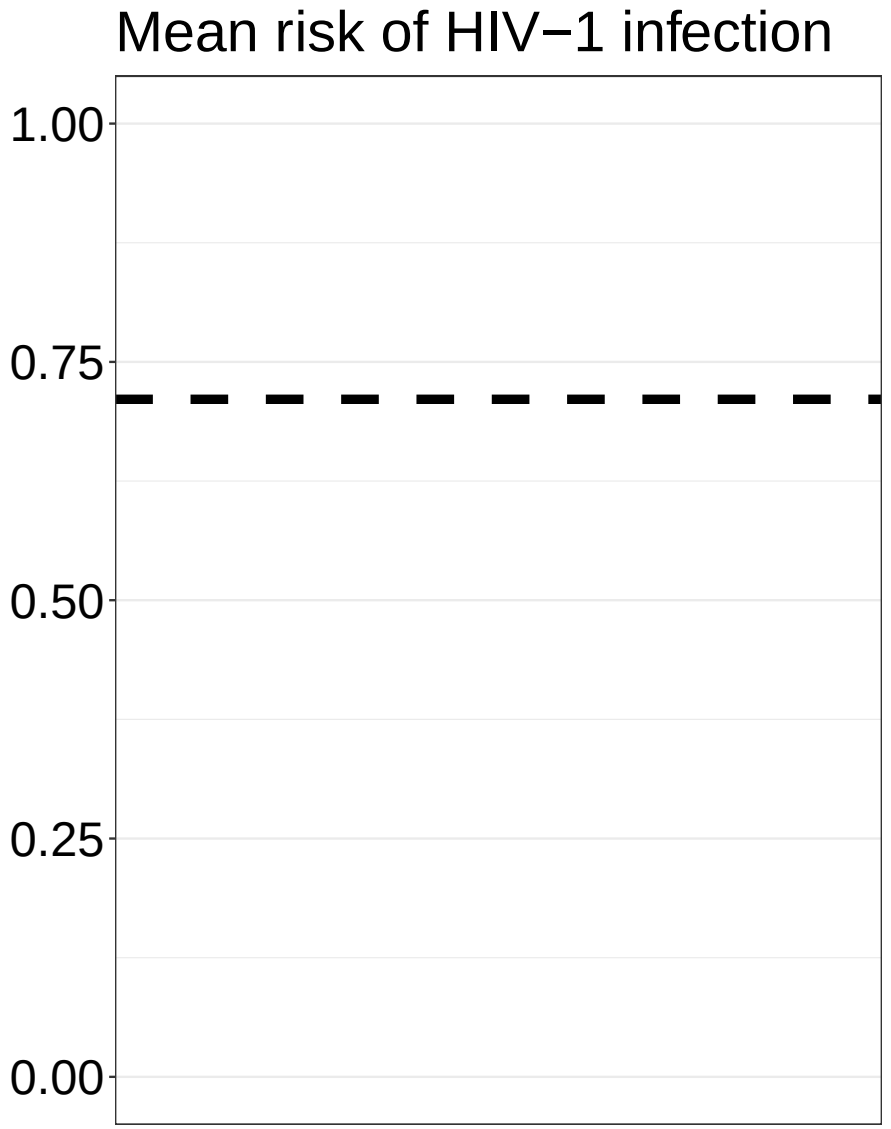

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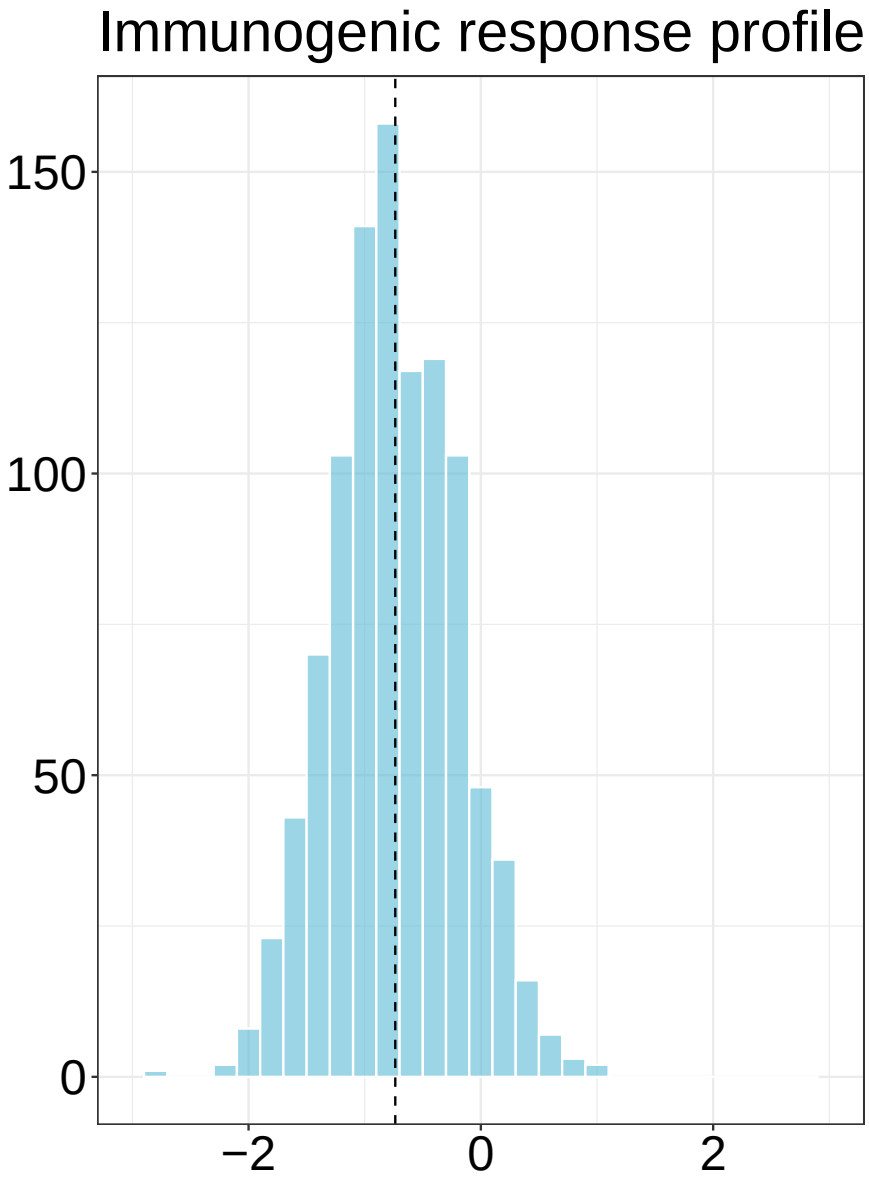

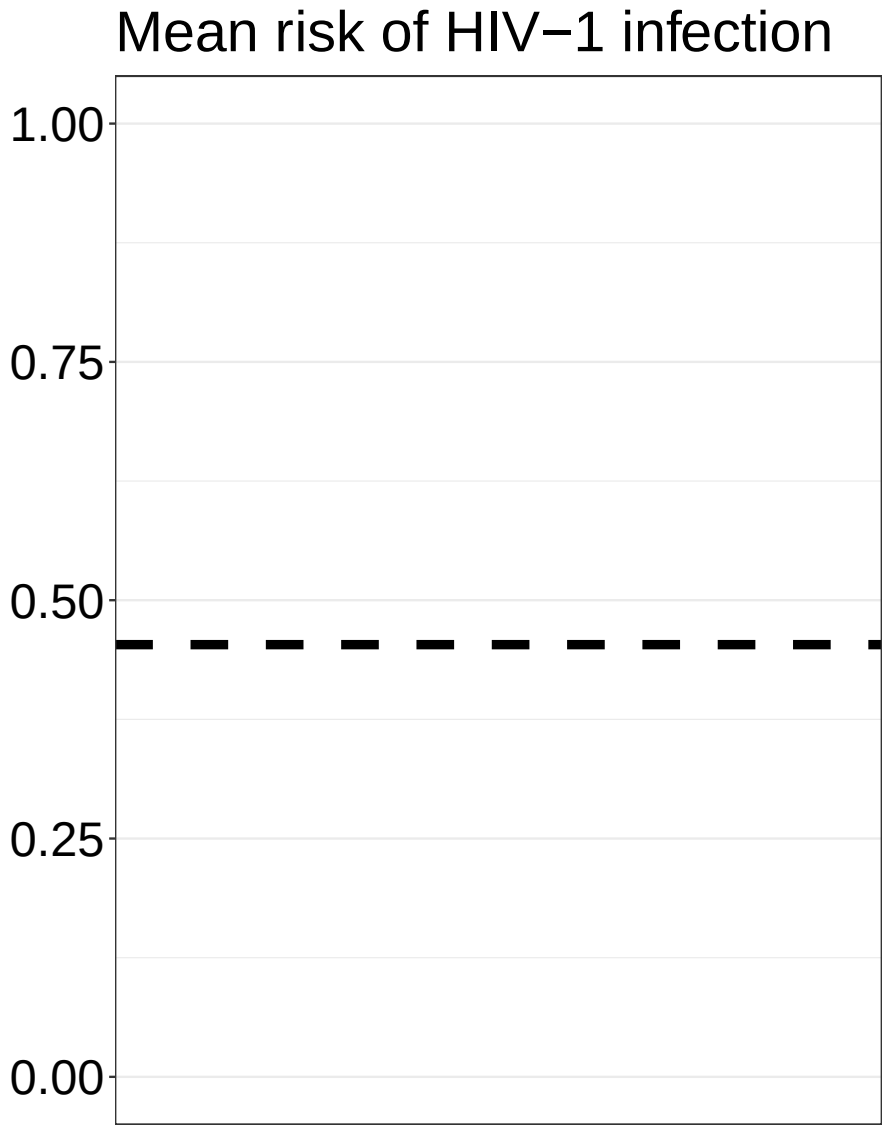

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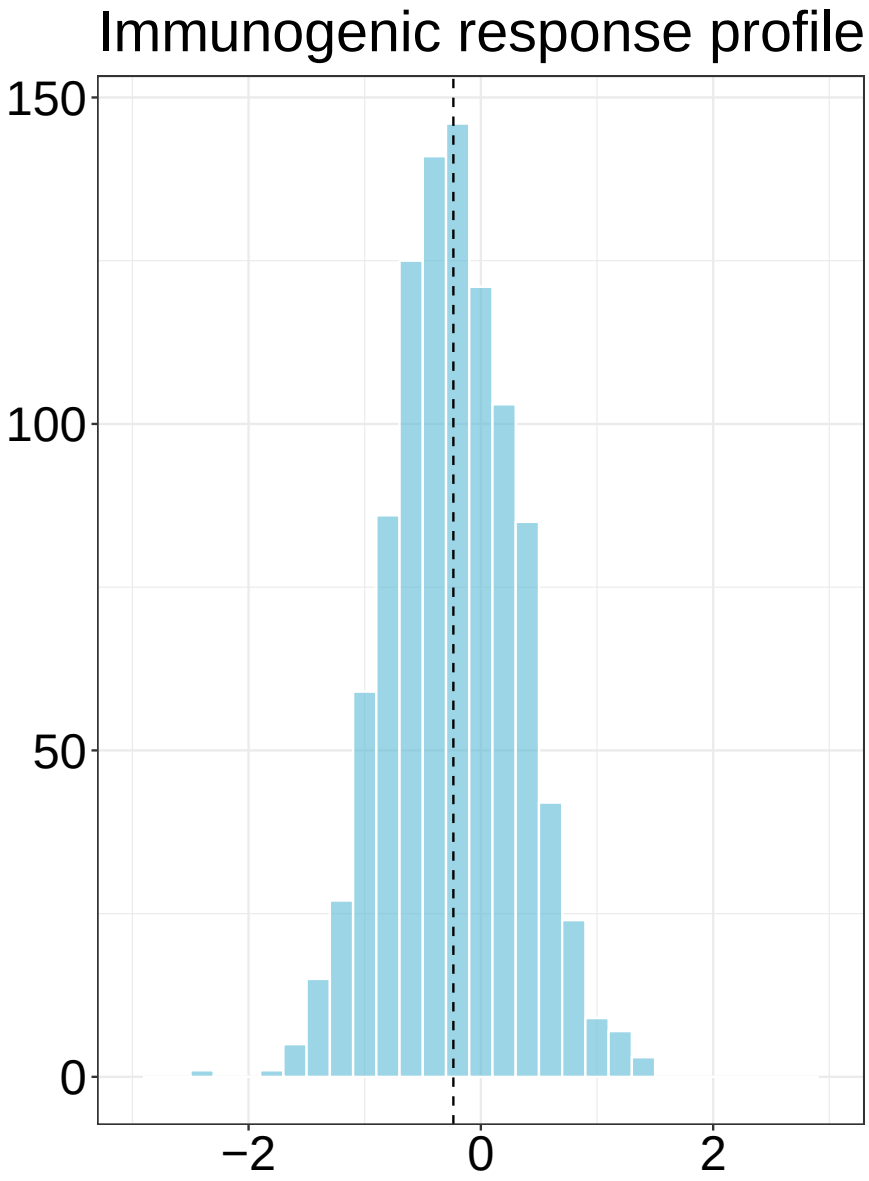

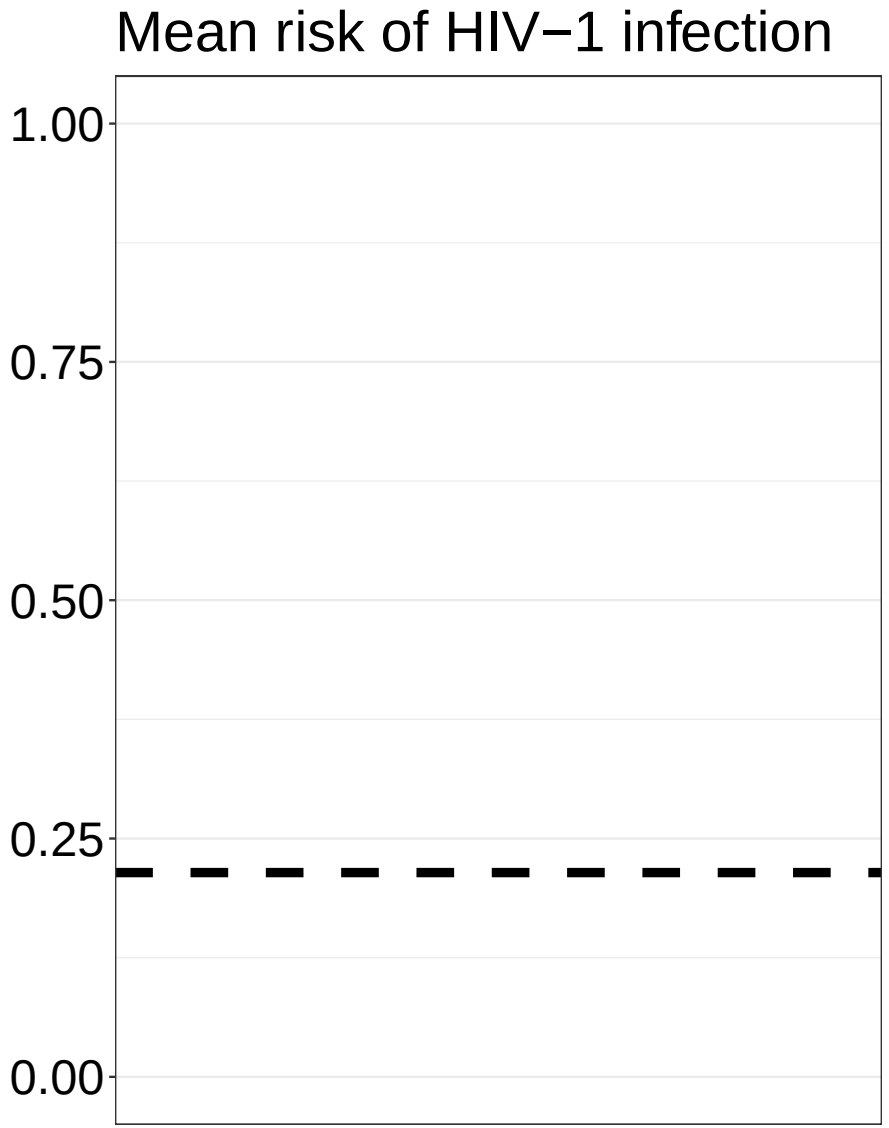

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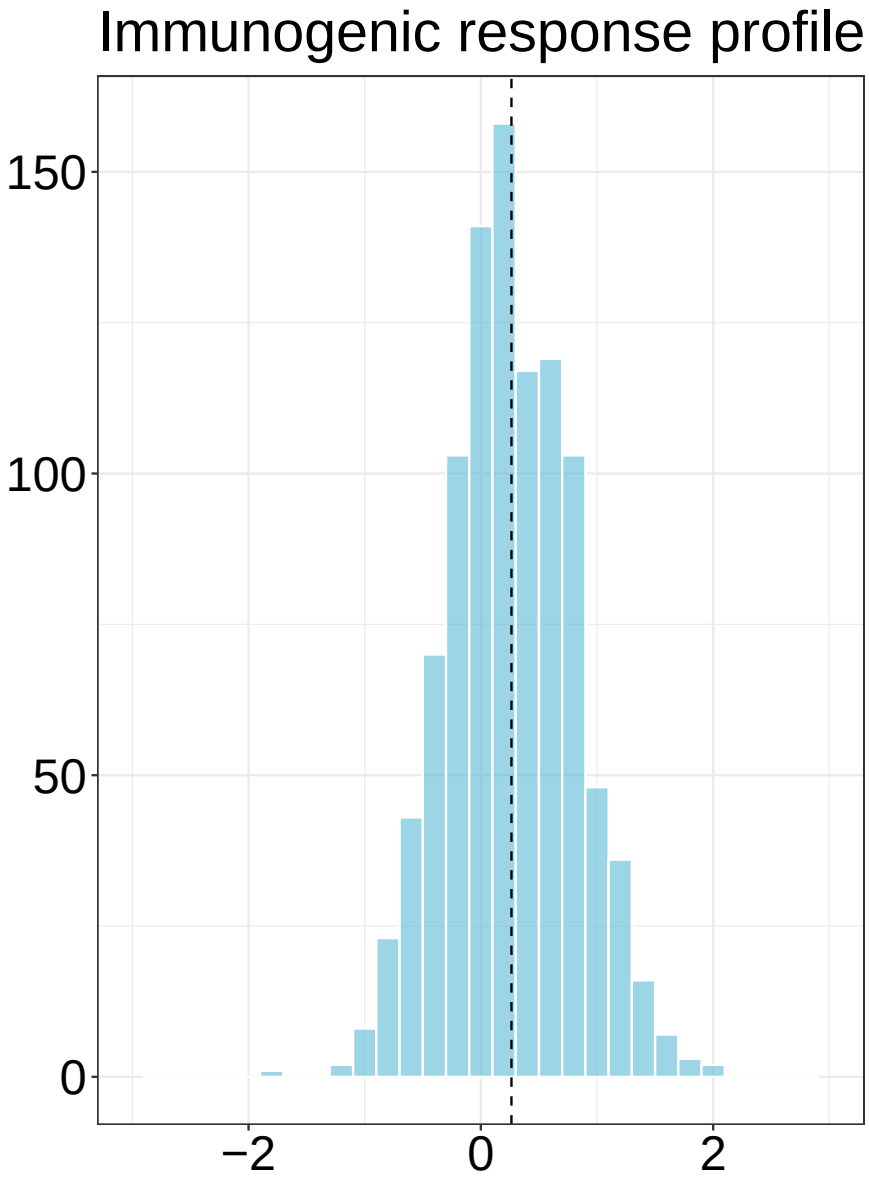

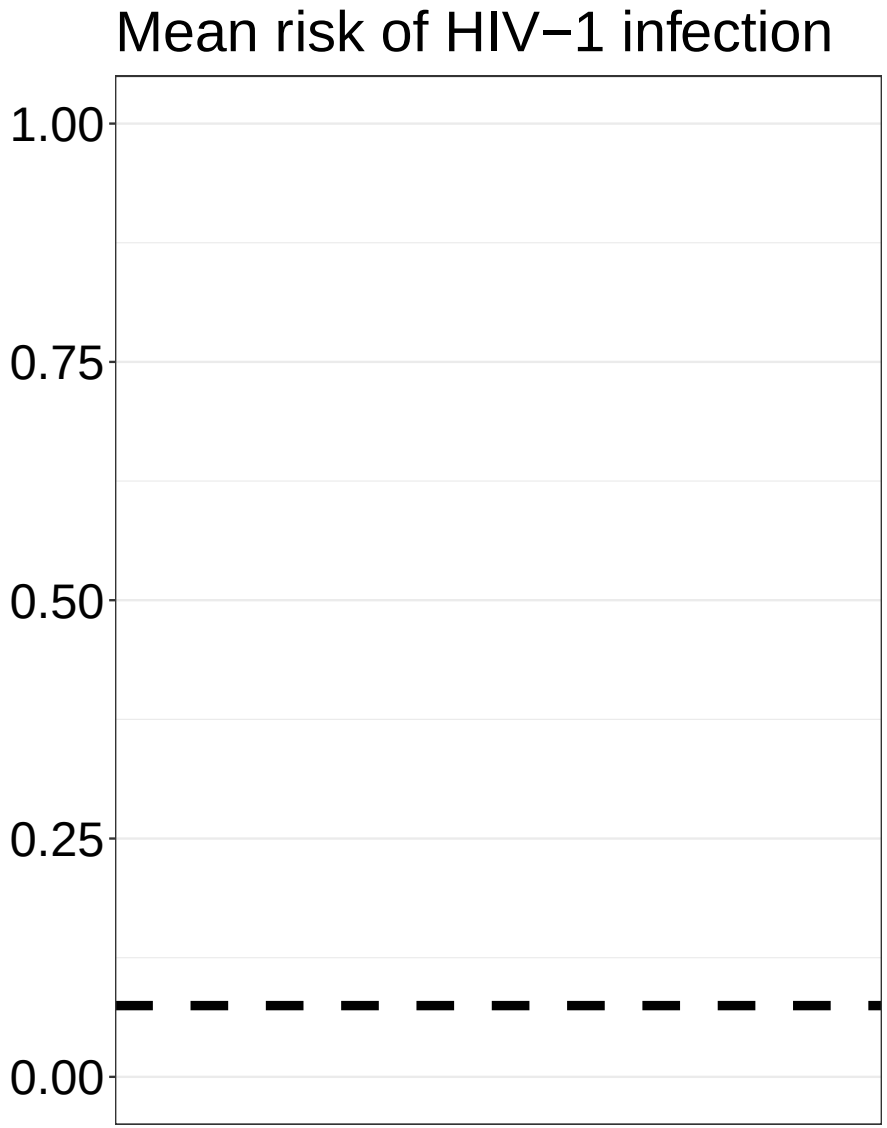

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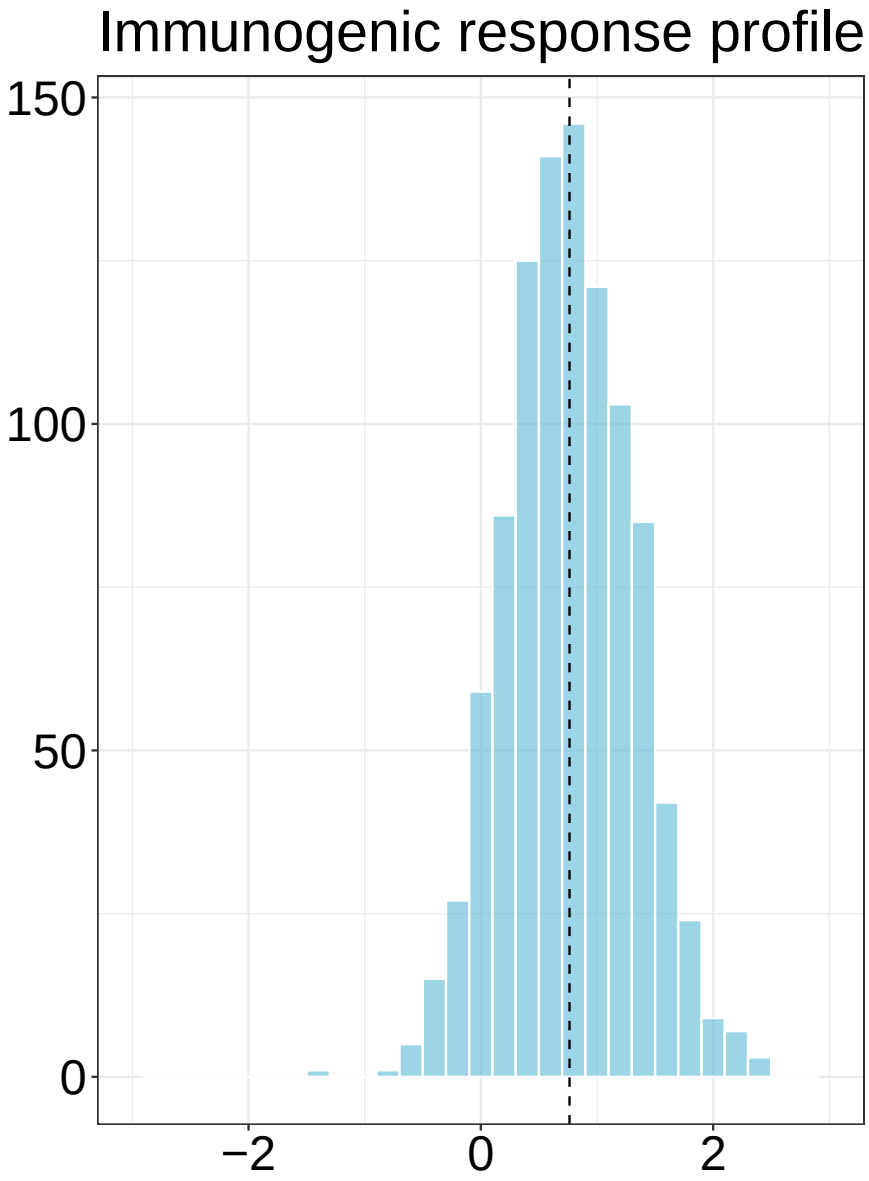

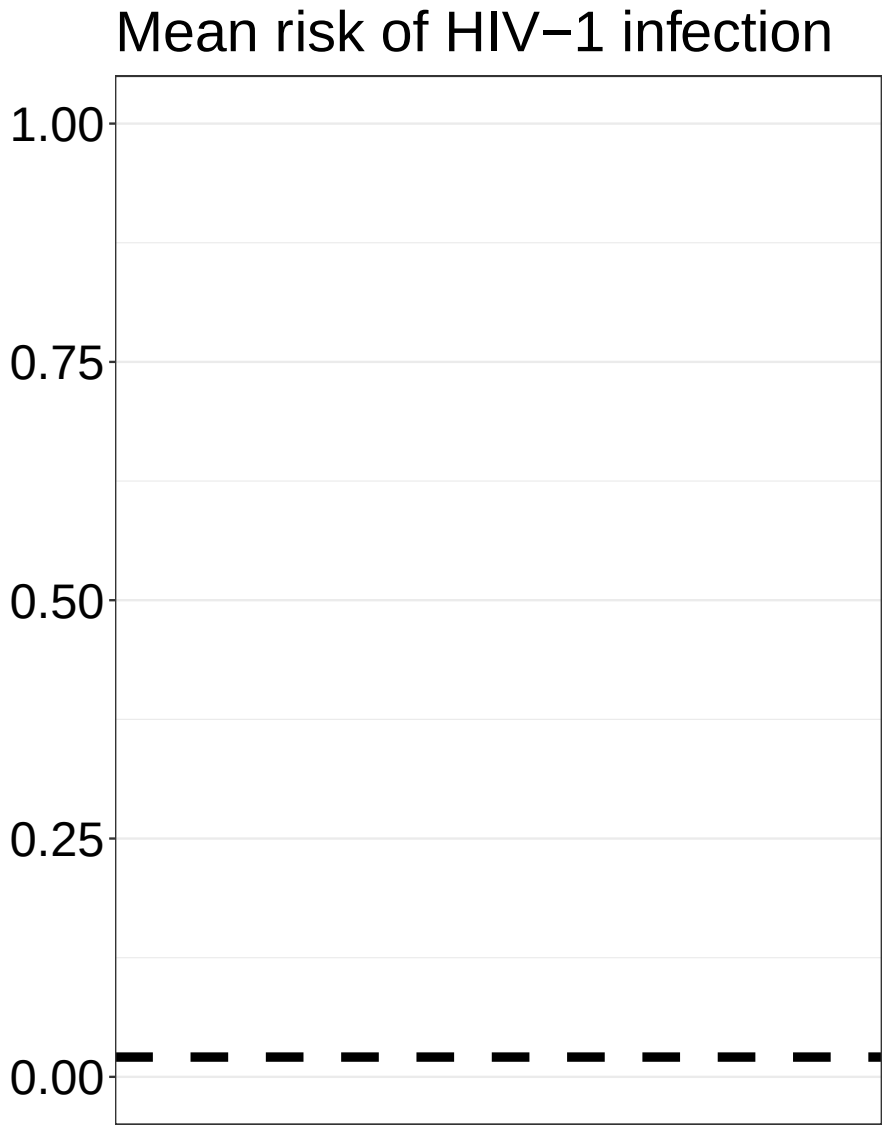

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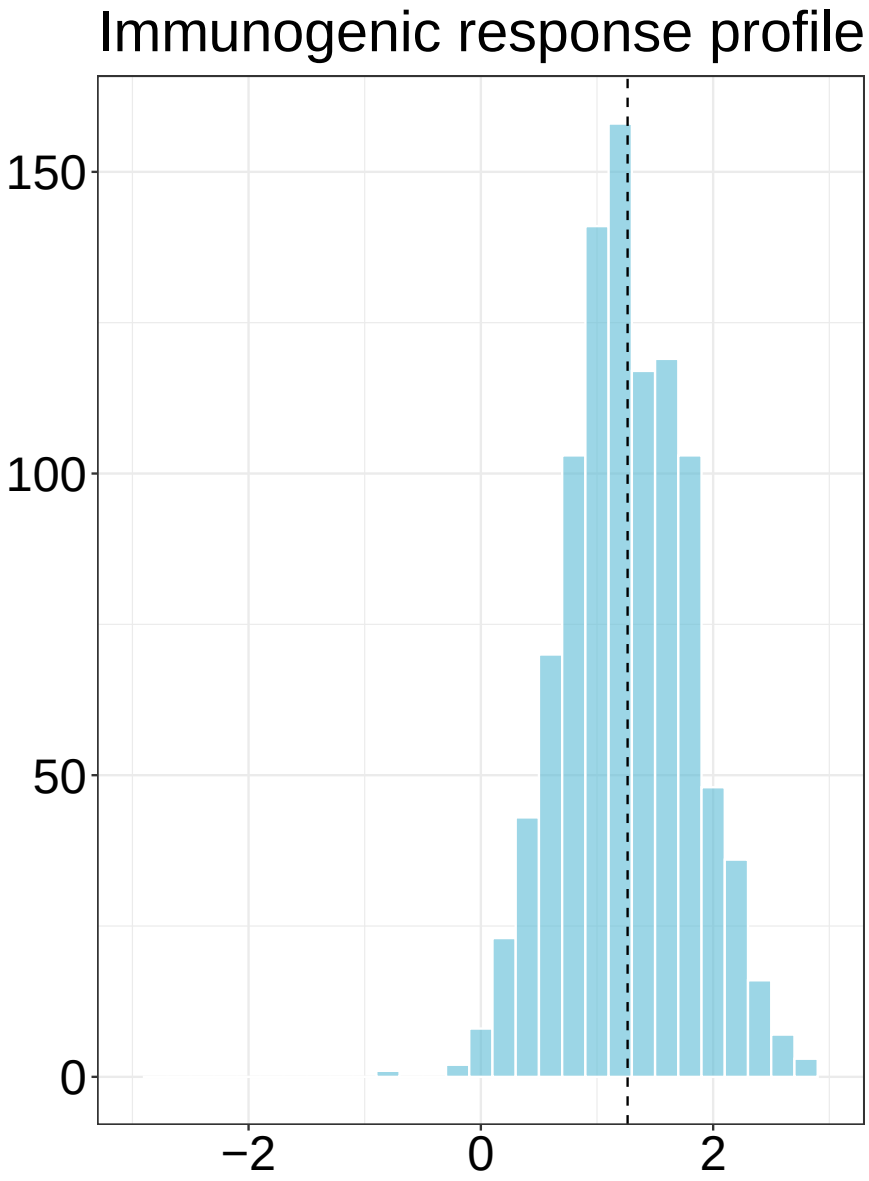

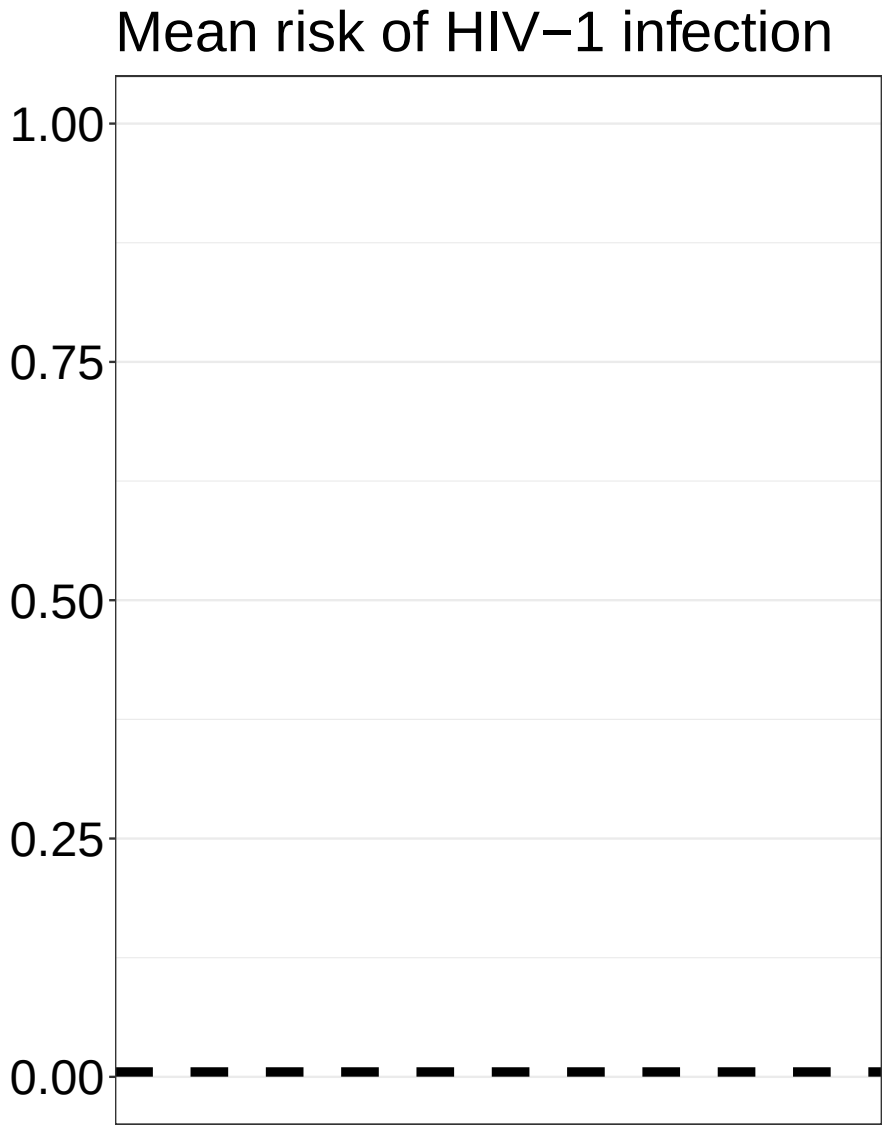

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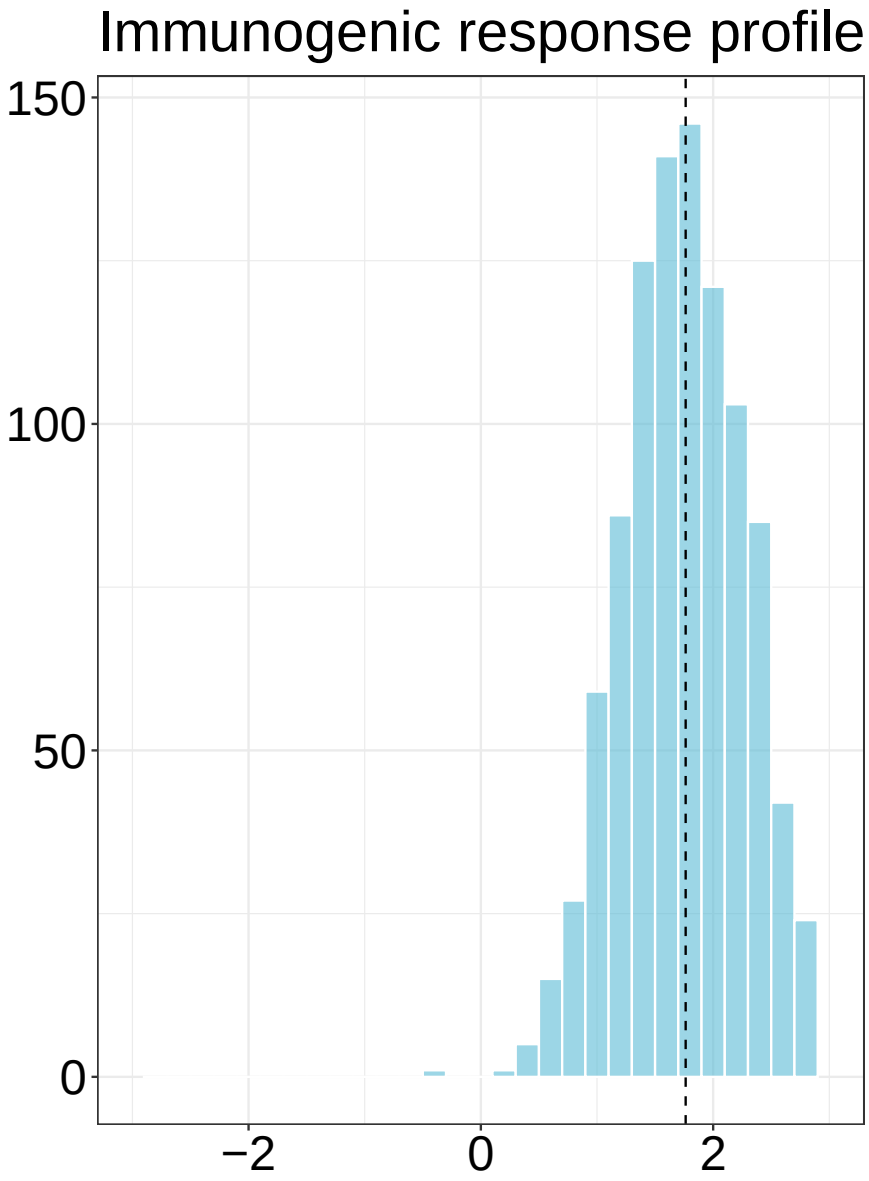

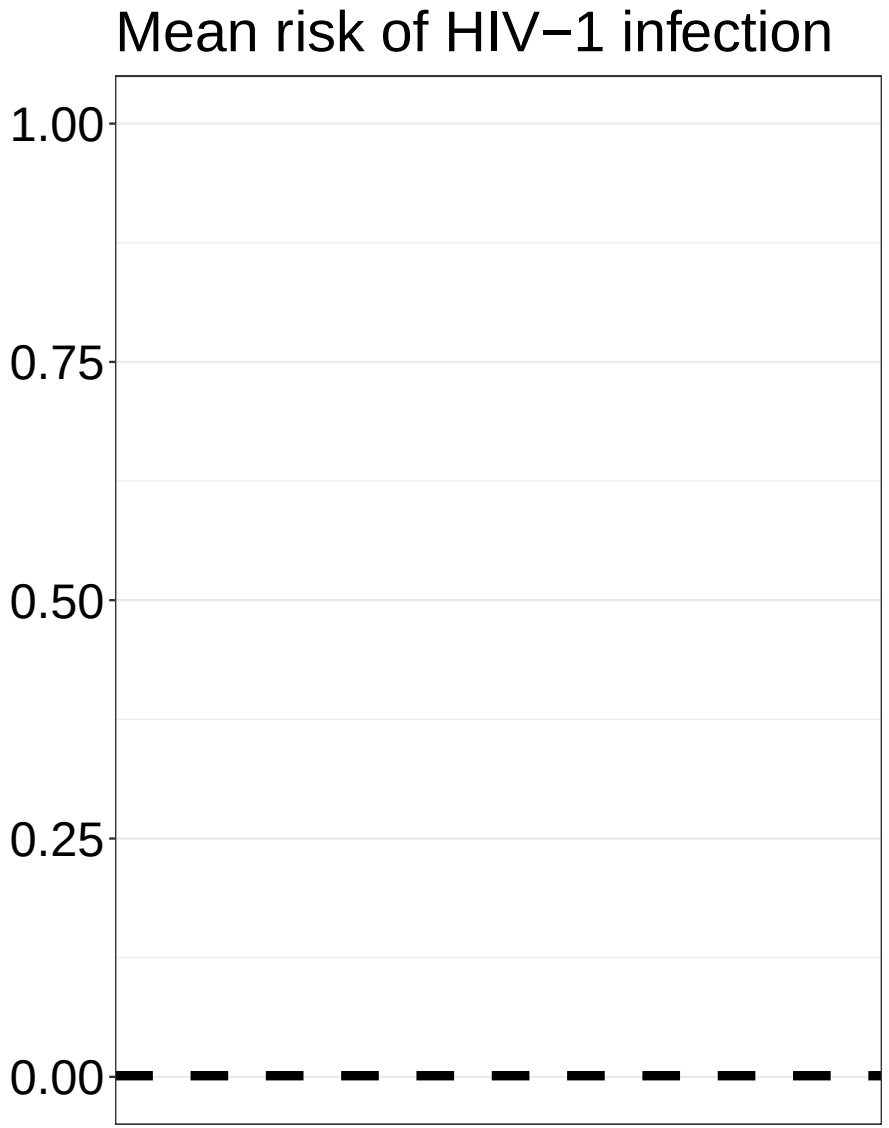

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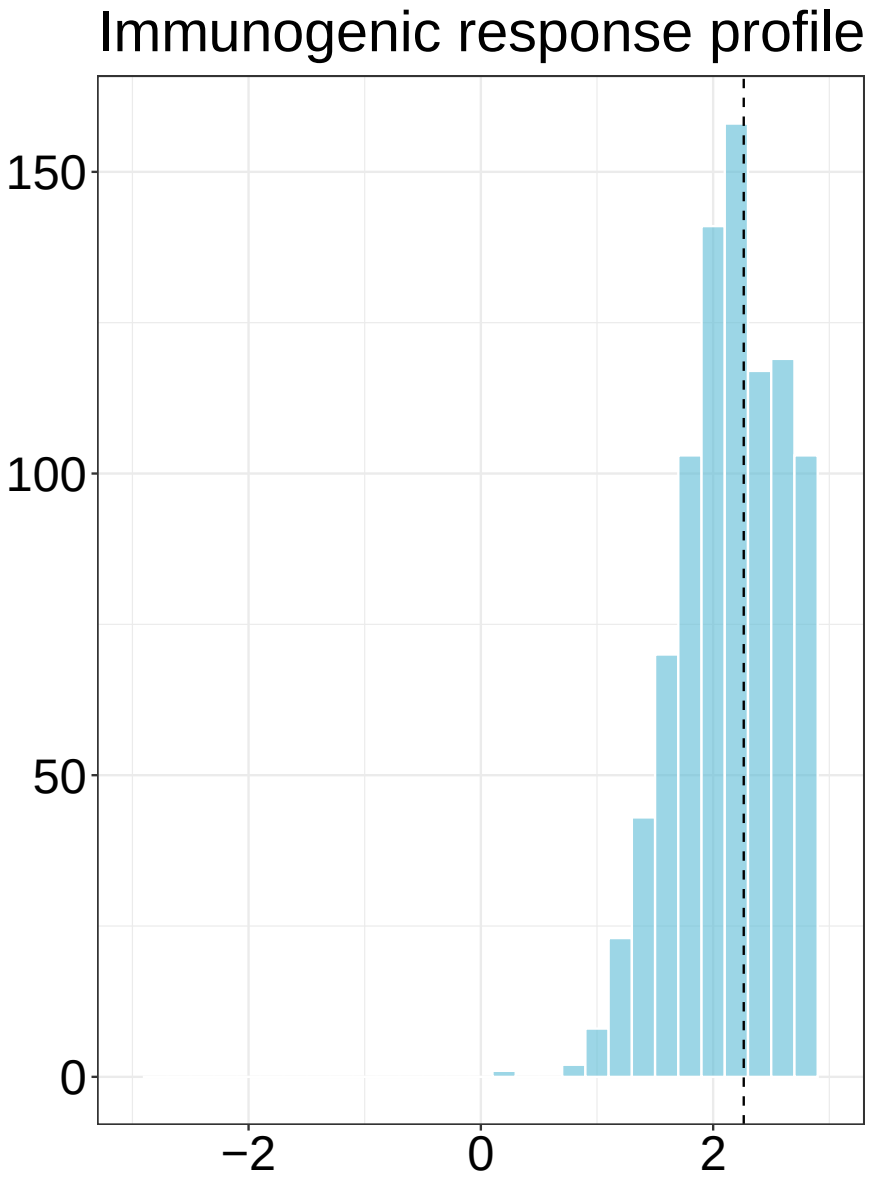

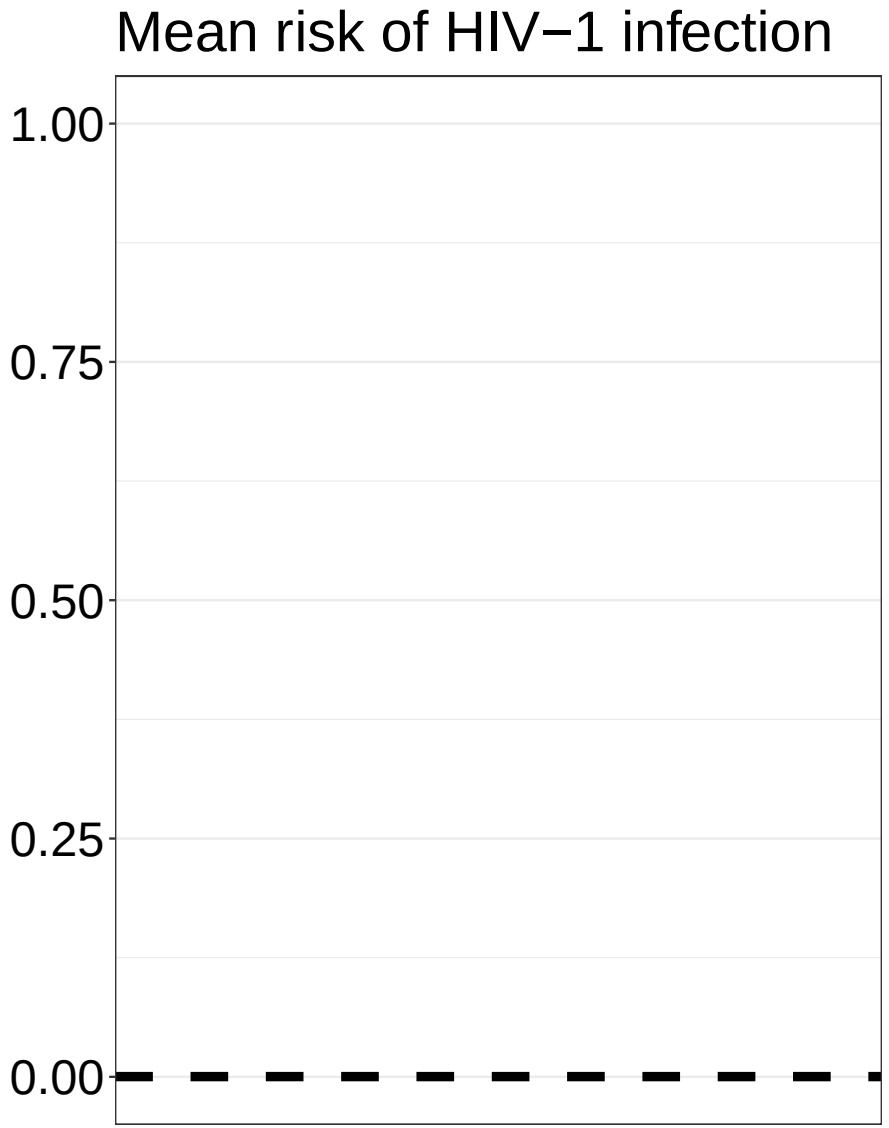

Flexible, efficient estimation

- The efficient influence function (EIF) is:

$$D(P_0^X)(x) = H(s, l)(y - \overline{Q}(s, l)) + \overline{Q}(d(s, l), l) - \Psi(P_0^X).$$

- The one-step estimator corrects bias by adding the empirical mean of the estimated EIF to the substitution estimator:

$$\Psi_n^+ = \frac{1}{n} \sum_{i=1}^{n} \overline{Q}_n(d(S_i, L_i), L_i) + D_n(O_i).$$

- The TML estimator updates initial estimates of $\overline{Q}_n$ by tilting:

$$\Psi_n^\star = \frac{1}{n} \sum_{i=1}^{n} \overline{Q}_n^\star(d(S_i, L_i), L_i).$$

- Both estimators are doubly robust.

Augmented estimators for two-phase sampling designs

- Rose and van der Laan (2011) introduce the IPCW-TMLE, to be used when observed data is subject to two-phase sampling.
- *Initial proposal:* correct for two-phase sampling by using a loss function with inverse probability of censoring weights:

$$\mathcal{L}(P_0^X)(O) = \frac{C}{\pi_0(Y, L)} \mathcal{L}^F(P_0^X)(X)$$

- When the sampling mechanism $\pi_0(Y, L)$ can be estimated by a parametric form, this procedure yields an efficient estimator.
- However, when machine learning is used (e.g., when $\pi_0(Y, L)$ is not *known by design*), this is insufficient.

Efficient estimation and multiple robustness

- Then, the IPCW augmentation must be applied to the EIF:

$$D(P_0^X)(o) = \frac{c}{\pi_0(y,l)} D^F(P_0^X)(x) - \left(1 - \frac{c}{\pi_0(y,l)}\right) \cdot \mathbb{E}(D^F(P_0^X)(x) \mid C = 1, Y = y, L = l),$$

  - Expresses observed data EIF $D^F(P_0^X)(o)$ in terms of full data EIF $D^F(P_0^X)(x)$; inclusion of second term ensures efficiency.
  - The expectation of the full data EIF $D^F(P_0^X)(x)$, taken only over units selected by the sampling mechanism (i.e., $C = 1$).

- A unique multiple robustness property — combinations of $(g_0(L), \overline{Q}_0(S, L)) \times (\pi_0(Y, L), \mathbb{E}(D^F(P_0^X)(x) \mid C = 1, Y, L))$.

Fighting the HIV-1 epidemic with preventive vaccines

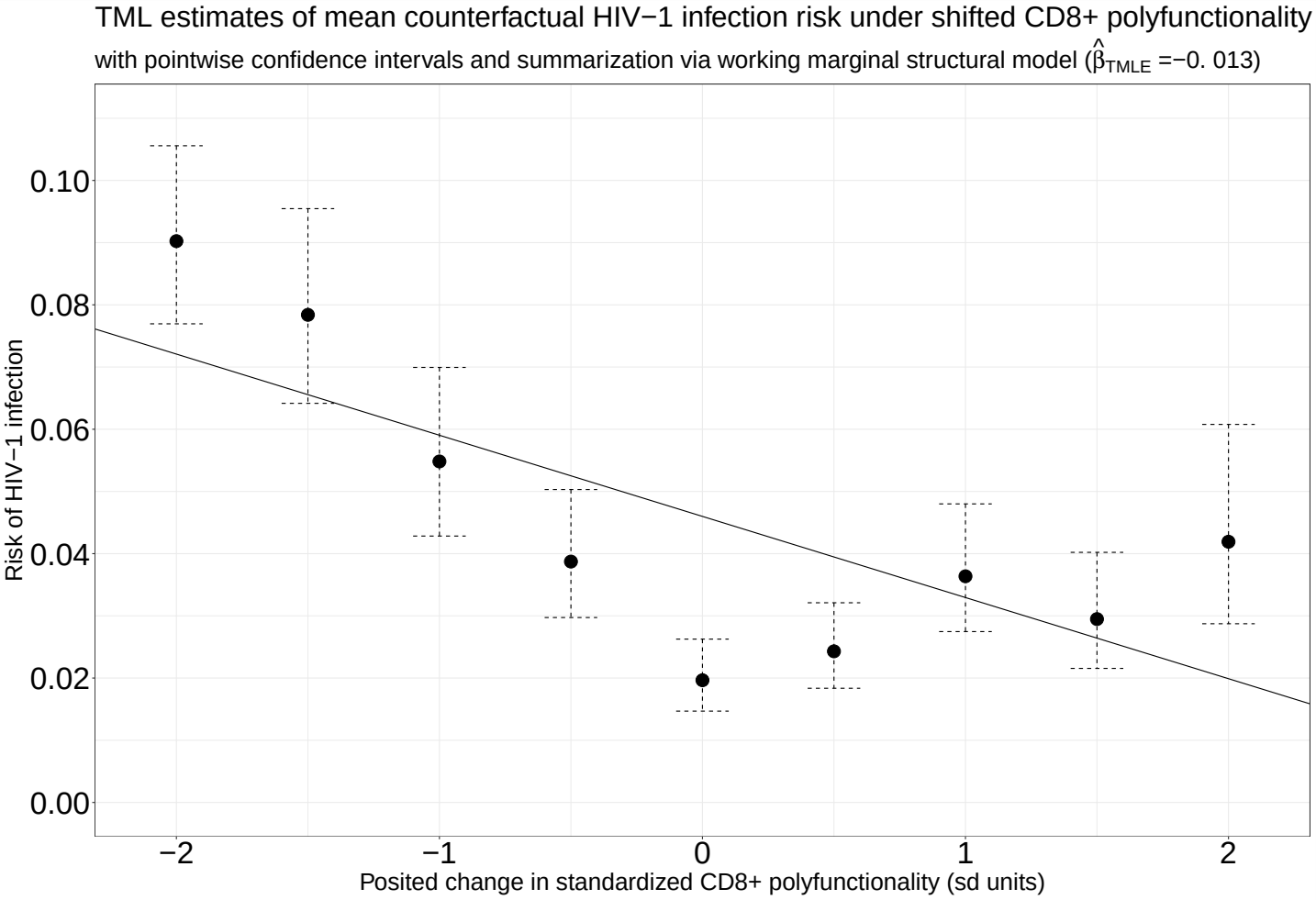

Figure 1: Analysis of HIV-1 risk as a function of CD8+ immunogenicity, using `R` package `txshift` (`https://github.com/nhejazi/txshift`).

Big picture takeaways

- Vaccine efficacy evaluation helps to develop enhanced vaccines better informed by biological properties of the target disease.
- HIV-1 vaccines modulate immunogenic response profiles as part of their mechanism for lowering HIV-1 infection risk.
- *Stochastic* interventions constitute a flexible framework for considering **realistic** treatment/intervention policies.
- Large-scale (vaccine) trials often use two-phase designs — need to (carefully!) accommodate for sampling complications.
- We've developed robust, open source statistical software for assessing stochastic interventions in observational studies.

Thank you!

https://nimahejazi.org

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https://github.com/nhejazi

https://doi.org/10.1111/biom.13375

At Warp Speed – COVID-19 Vaccine Trials

COVID-19 Vaccine Development

- *Nucleic acid vaccines*: Moderna (mRNA), Pfizer (mRNA)
- *Viral-vectored vaccines*: AstraZeneca (chimpanzee adenovirus), Janssen (human adenovirus)
- *Subunit vaccines*: NovaVax, Sanofi / GlaxoSmithKline
- *Weakened/inactivated vaccines*: Sinopharm, Sinovac

Operation Warp Speed (OWS)

- Do we have the time? Polio (7 years), Measles (9 years), Chickenpox (34 years), Mumps (4 years), HPV (15 years).
- OWS: "300M doses of safe, effective vaccine by 01 Jan. 2021".
- How? Typical process timeline (73 months) replaced by an *accelerated* process of 14 months.
- COVID-19 Prevention Network (CoVPN):
  - formed by NIAID to establish a unified clinical trial network for evaluating vaccines and monoclonal antibodies.
  - Statisticians: primary trial design/analysis, sequential efficacy monitoring, safety monitoring, immune correlates.

Immune Correlates of Protection (Plotkin and Gilbert 2012)

- Correlate of Protection (CoP): immune marker statistically predictive of vaccine efficacy, not necessarily mechanistic.
- Mechanistic CoP (mCoP): immune marker that is causally and mechanistically responsible for protection.
- Nonmechanistic CoP (nCoP): immune marker that is predictive but not a causal agent of protection.
- A CoP is a *candidate surrogate* endpoint (Prentice 1989) — primary endpoint in future trials if reliably predictive.

Measuring Correlates: Two-Phase Designs

- Running assays on $> 30,000$ blood draws is timely, expensive, and, as it turns out, statistically unnecessary.
- Instead we measure immune responses via a case-cohort design (Prentice 1986):
  - a stratified random subcohort (≈ 1600 individuals)
  - all SARS-CoV-2 and COVID endpoints.
- Case-cohort designs are a special case of two-phase sampling (Breslow et al. 2003; 2009):
  - Phase 1: measure baseline, vaccine, endpoint on everyone.
  - Phase 2: given baseline, vaccine, endpoint, select members of immune response subcohort with (possibly known) probability.

Stochastic–Interventional Vaccine Efficacy

- Causal parameter based on vaccine efficacy (VE) estimands:

$$\mathrm{SVE}(\delta) = 1 - \frac{\mathbb{E}[\mathbb{P}(Y = 1 \mid A = 1, S = s + \delta, L = l) \mid A = 1, L]}{\mathbb{P}(Y(0) = 1)}.$$

- $\mathbb{P}(Y(0) = 1)$: counterfactual infection risk in the placebo arm — under randomization, $\mathbb{P}(Y(0) = 1) = \mathbb{P}(Y = 1 \mid A = 0)$.
- Summarizes VE thru stochastic interventions indexed by δ.
- Further details in CoVPN's public immune correlates SAP at `https://doi.org/10.6084/m9.figshare.13198595`.

Additional Complexities of Two-Phase Designs

- Observed data structure: $O = (L, A, Z, CS, Y, C)$
  - $A \in \{0, 1\}$: randomized vaccination assignment
  - Z: post-vaccination confounder (e.g., unblinded risky behavior)
  - S: candidate mCoPs (causal mediators)
  - Y: symptomatic SARS-CoV-2 infection
  - $C := f(Y, L)$: selection into second-phase sample
- But what about $O = (L, A, Z, CS, \Delta, \widetilde{T}, C)$?
  - $\widetilde{T} = \min(T_F, T_C)$: possibly right-censored time to infection
  - $\Delta = \mathbb{I}(T_F < T_C)$: symptomatic SARS-CoV-2 infection
  - Can C still be a function of $\widetilde{T}$?

Causal Mediation Analysis: Explanation and Mechanism

- Identification assumptions:
  - A1: No unmeasured confounding of $\{A, Y\}$ relationship.
  - A2: No unmeasured confounding of $\{S, Y\}$ relationship.
  - A3: No unmeasured confounding of $\{A, S\}$ relationship.
  - A4: No $\{S, Y\}$ confounder affected by A, i.e., no Z.

- *Indirect* effects: thru pathways involving candidate mCoPs.
  - Natural (in)direct effects (Robins and Greenland 1992, Pearl 2013): binary A and S, no Z, "cross-world" independence.
  - Stochastic (in)direct effects (Díaz and Hejazi 2020): continuous A and S, no Z; no "cross-world" exclusion.
  - Interventional (in)direct effects (Díaz et al. 2020): binary A, continuous S, Z OK, no "cross-world" exclusion.
  - Stochastic interventional (in)direct effects (Hejazi et al. 2020): continuous A and S, Z ok, no "cross-world" exclusion.

Appendix

Literature: Haneuse and Rotnitzky (2013)

- *Proposal:* Characterization of stochastic interventions as *modified treatment policies* (MTPs).
- Assumption of *piecewise smooth invertibility* allows for the intervention distribution of any MTP to be recovered:

$$g_{0,\delta}(s \mid l) = \sum_{j=1}^{J(l)} I_{\delta,j}\{h_j(s,l), l\} g_0\{h_j(s,l) \mid l\} h_j'(s,l)$$

- Such intervention policies account for the natural value of the intervention S directly yet are interpretable as the imposition of an altered intervention mechanism.
- Identification conditions for assessing the parameter of interest under such interventions appear technically complex (at first).

Literature: Young et al. (2014)

- Establishes equivalence between g-formula when proposed intervention depends on natural value and when it does not.
- This equivalence leads to a sufficient positivity condition for estimating the counterfactual mean under MTPs via the same statistical functional studied in Díaz and van der Laan (2012).
- Extends earlier identification results, providing a way to use the same statistical functional to assess $\mathbb{E}Y_{d(S,L)}$ or $\mathbb{E}Y_{d(L)}$.
- The authors also consider limits on implementing shifts $d(S, L)$, and address working in a longitudinal setting.

Literature: Díaz and van der Laan (2018)

- Builds on the original proposal, accomodating MTP-type shifts $d(S, L)$ proposed after their earlier work.
- To protect against positivity violations, considers a specific shifting mechanism:

$$d(s, l) = \begin{cases} s + \delta, & s + \delta < u(l) \\ s, & \text{otherwise} \end{cases}$$

- Proposes an improved TMLE algorithm, with a single auxiliary covariate for constructing the TML estimator.

Nonparametric conditional density estimation

- To compute the auxiliary covariate $H(s, l)$, we need to estimate conditional densities $g(S \mid L)$ and $g(S - \delta \mid L)$.
- There is a rich literature on density estimation, we follow the approach proposed in Díaz and van der Laan (2011).
- To build a conditional density estimator, consider

$$g_{n,\alpha}(s \mid L) = \frac{\mathbb{P}(S \in [\alpha_{t-1}, \alpha_t) \mid L)}{\alpha_t - \alpha_{t-1}},$$

  for $\alpha_{t-1} \leq s < \alpha_t$.

  - This is a classification problem, where we estimate the probability that a value of S falls in a bin $[\alpha_{t-1}, \alpha_t)$.
  - The choice of the tuning parameter t corresponds roughly to the choice of bandwidth in classical kernel density estimation.

Nonparametric conditional density estimation

- Díaz and van der Laan (2011) propose a reformulation of this classification approach as a set of hazard regressions.
- To effectively employ this proposed reformulation, consider

$$\mathbb{P}(S \in [\alpha_{t-1}, \alpha_t) \mid L) = \mathbb{P}(S \in [\alpha_{t-1}, \alpha_t) \mid S \geq \alpha_{t-1}, L) \times \Pi_{j=1}^{t-1}\{1 - \mathbb{P}(S \in [\alpha_{j-1}, \alpha_j) \mid S \geq \alpha_{j-1}, L)\}$$

  - The likelihood of this model may be expressed to correspond to the likelihood of a binary variable in a data set expressed via a long-form repeated measures structure.
  - Specifically, the observation of X_i is repeated as many times as intervals $[\alpha_{t-1}, \alpha_t)$ are before the interval to which S_i belongs, and the binary variables indicating $S_i \in [\alpha_{t-1}, \alpha_t)$ are recorded.

Density estimation with the Super Learner algorithm

- To estimate $g(S \mid L)$ and $g(S - \delta \mid L)$, use a pooled hazard regression, spanning the support of S.
- We rely on the Super Learner algorithm of van der Laan et al. (2007) to build an ensemble learner that optimally weights each of the proposed regressions, using cross-validation (CV).
- The Super Learner algorithm uses V-fold CV to train each proposed regression model, weighting each by the inverse of its average risk across all V holdout sets.
- By using a library of regression estimators, we invoke the result of van der Laan et al. (2004), who prove this likelihood-based cross-validated estimator to be asymptotically optimal.

Key properties of TML estimators

- **Asymptotic linearity:**

$$\Psi(P_n^\star) - \Psi(P_0^X) = \frac{1}{n}\sum_{i=1}^{n} D(P_0^X)(X_i) + o_P\left(\frac{1}{\sqrt{n}}\right)$$

- **Gaussian limiting distribution:**

$$\sqrt{n}(\Psi(P_n^\star) - \Psi(P_0^X)) \to N(0, Var(D(P_0^X)(X)))$$

- **Statistical inference:**

$$\text{Wald-type confidence interval} : \Psi(P_n^\star) \pm z_{1-\frac{\alpha}{2}} \cdot \frac{\sigma_n}{\sqrt{n}},$$

where σ_n^2 is computed directly via $\sigma_n^2 = \frac{1}{n}\sum_{i=1}^{n} D^2(\cdot)(X_i)$.

Algorithm for TML estimation

1. Construct initial estimators g_n of $g_0(S, L)$ and Q_n of $\overline{Q}_0(S, L)$, perhaps using data-adaptive regression techniques.
2. For each observation i, compute an estimate $H_n(s_i, l_i)$ of the auxiliary covariate $H(s_i, l_i)$.
3. Estimate the parameter ϵ in the logistic regression model

$$\text{logit}\overline{Q}_{\epsilon,n}(s, l) = \text{logit}\overline{Q}_n(s, l) + \epsilon H_n(s, l),$$

   or an alternative regression model incorporating weights.
4. Compute TML estimator Ψ_n of the target parameter, defining update $\overline{Q}_n^\star$ of the initial estimate $\overline{Q}_{n,\epsilon_n}$:

$$\Psi_n = \Psi(P_n^\star) = \frac{1}{n}\sum_{i=1}^{n}\overline{Q}_n^\star(d(S_i, L_i), L_i).$$

Algorithm for IPCW-TML estimation

1. Using all observed units (X), estimate sampling mechanism $\pi(Y, L)$, perhaps using data-adaptive regression methods.

2. Using only observed units in the second-stage sample $C = 1$, construct initial estimators $g_n(S, L)$ and $\overline{Q}_n(S, L)$, weighting by the sampling mechanism estimate $\pi_n(Y, L)$.

3. With the approach described for the full data case, compute $H_n(s_i, l_i)$, and fluctuate submodel via logistic regression.

4. Compute IPCW-TML estimator Ψ_n of the target parameter, by solving the IPCW-augmented EIF estimating equation.

5. Iteratively update estimated sampling weights $\pi_n(Y, L)$ and IPCW-augmented EIF, updating TML estimate in each iteration, until $\frac{1}{n}\sum_{i=1}^{n} \text{EIF}_i < \frac{1}{n}$.

Identifying the best efficient estimator

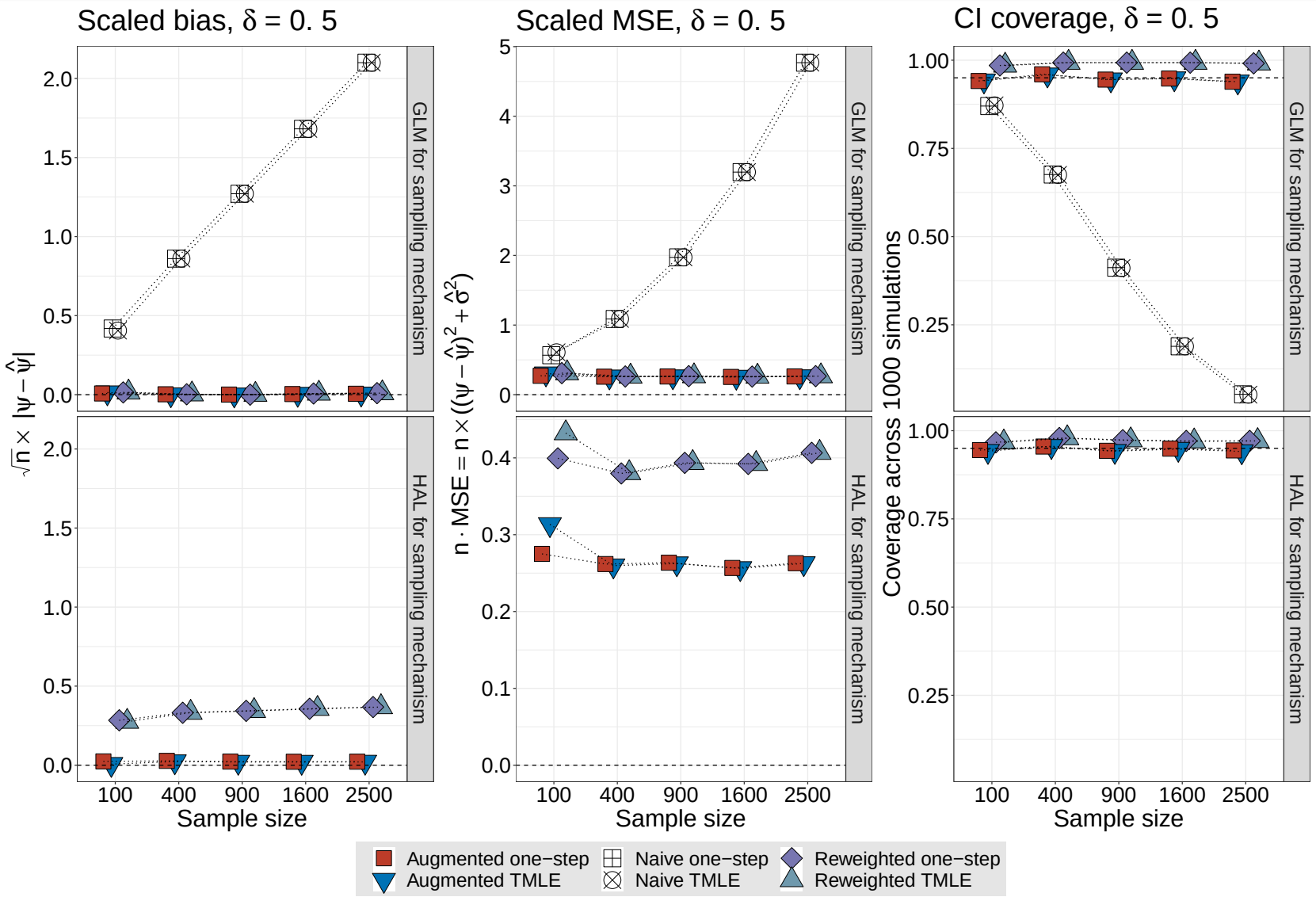

Figure 2: Relative performance of reweighted and augmented estimators.

A linear modeling perspective

- Briefly consider a simple data structure: $X = (Y, S)$; we seek to model the outcome Y as a function of S.
- To posit a linear model, consider $Y_i = \beta_0 + \beta_1 S_i + \epsilon_i$, with error $\epsilon_i \sim N(0, 1)$.
- Letting δ be a change in S, $Y_{S+\delta} - Y_S$ may be expressed

$$\begin{aligned}
\mathbb{E}Y_{S+\delta} - \mathbb{E}Y_S &= [\beta_0 + \beta_1(\mathbb{E}S + \delta)] - [\beta_0 + \beta_1(\mathbb{E}S)] \\
&= \beta_0 - \beta_0 + \beta_1 \mathbb{E}S - \beta_1 \mathbb{E}S + \beta_1 \delta \\
&= \beta_1 \delta
\end{aligned}$$

- Thus, a *unit shift* in S (i.e., $\delta = 1$) may be seen as inducing a change in the difference in outcomes of magnitude β_1.

A causal inference perspective

- Consider a data structure: $(Y_s, s \in \mathcal{S})$.
- To posit a linear model, let $Y_s = \beta_0 + \beta_1 s + \epsilon_s$ for $s \in \mathcal{S}$, with error $\epsilon_s \sim N(0, \sigma_s^2)$ $\forall s \in S$.
- For the counterfactual outcomes $(Y_{s'+\delta}, Y_{s'})$, their difference, $Y_{s'+\delta} - Y_{s'}$, for some $s' \in \mathcal{S}$, may be expressed

$$\begin{aligned}\mathbb{E}Y_{s'+\delta} - \mathbb{E}Y_{s'} &= [\beta_0 + \beta_1(s' + \delta) + \mathbb{E}\epsilon_{s'+\delta}] - [\beta_0 + \beta_1 s' + \mathbb{E}\epsilon_{s'}] \\ &= \beta_1 \delta\end{aligned}$$

- Thus, a *unit shift* for $s' \in S$ (i.e., $\delta = 1$) may be seen as inducing a change in the difference in the counterfactual outcomes of magnitude β_1.

Slope in a semiparametric model

- Consider the stochastic intervention $g^\star(\cdot \mid L)$:

$$\begin{aligned}\mathbb{E}Y_{g^\star} &= \int_L \int_s \mathbb{E}(Y \mid S = s, L) g(s - \delta \mid L) \cdot ds \cdot dP_0(L) \\ &= \int_L \int_z \mathbb{E}(Y \mid S = z + \delta, L) g(z \mid L) \cdot dz \cdot dP_0(L),\end{aligned}$$

  defning the change of variable $z = s - \delta$.

- For a semiparametric model, $\mathbb{E}(Y \mid S = z, L) = \beta z + \theta(L)$:

$$\begin{aligned}\mathbb{E}Y_{g^\star} - \mathbb{E}Y &= \int_L \int_z [\mathbb{E}(Y \mid S = z + \delta, L) - \mathbb{E}(Y \mid S = z, L)] \\ &\qquad g(z \mid L) \cdot dz \cdot dP_0(L) \\ &= [\beta(z + \delta) + \theta(L)] - [\beta z + \theta(L)] \\ &= \beta\delta\end{aligned}$$

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