

## Bickel–Doksum. Mathematical Statistics. Volume I.

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### Errata

- p. xiii, l. 5. “terabytes” should be “terabytes”.
- p. xiv, l. -20. “Chapters 7–10” should be “Chapters 7–9”.
- p. 7, l. 13: Insert “a well defined parameter” after “we can define”.
- p. 9 In the statement of (2). Change “there exists a set  $\{x_1, x_2, \dots\}$  ... all  $\theta$ ” to “the set  $\{x_1, x_2, \dots\} = \{x : p(x, \theta) > 0\}$  is the same set for all  $\theta \in \Theta$ ”.
- p. 11, Ex. 1.1.5. Label the expression on line 9 as (1.1.4). On line 15, replace “model (a)” with “model (1.1.4)”.
- p. 14, l. -14. “Bayes rule” to “Bayes theorem”.
- p. 19, l. -7. Switch  $\mathcal{N}(\mu + \Delta, \sigma^2)$  with  $\mathcal{N}(\mu, \sigma^2)$ .
- p. 20, l. -16. After “of  $\hat{\nu}$ ”, insert “If  $\text{Bias}(\hat{\nu}) = 0$ , then  $\hat{\nu}$  is called *unbiased*”.
- p. 20, l. 8 and l. 10.  $\delta(\mathbf{x})$  should be  $\delta(\mathbf{X})$ .
- p. 20, l. 9, Change “ $l(P, \delta(X))$ ” to “ $l(P, \delta(X))$ ”.
- p. 20, l. -12. “[ $E(\hat{\nu}) - \mu$ ]” should be “[ $E(\hat{\nu}) - \nu$ ]”.
- p. 21, l. -14. “ $E(\hat{x} - \mu)^2$ ” should be “ $E(\hat{X} - \mu)^2$ ”.
- p. 21, l. 7. “ $n_0 = \sigma_0/\epsilon$ ” should be “ $n_0 = (\sigma_0/\epsilon)^2$ ”.
- p. 23, l. 12. After “providing a small bound ... to minimize the probability of a Type II error,” insert “The bound on the probability of a Type I error is called the *level of significance* and deciding  $\Theta_1$  is referred to as “Rejecting the hypothesis  $H : \theta \in \Theta_0$  at level of significance  $\alpha$ ”.
- p. 25, l. -8. “ $R(\theta_2\delta)$ ” should be “ $R(\theta_2, \delta)$ ” .
- p. 29, l. 16. “By (1.3.10)” should be “By (1.3.11)”.
- p. 34, l. -9. expansion of.
- p. 35,  $p(z, y)$  table. Should be “ $p(1, 0) = 0.025, p(1, 1) = 0.025$ ”.
- p. 35, Bottom of page, Last equation. “ $\sum_x$ ” should be “ $\sum_z$ ”.
- p. 39, Thm. 1.4.4. “best MSPE” should be “best linear MSPE”.
- p. 39, l. -8. “ $\mu_l(\mathbf{z})$ ” should be “ $\mu_l(\mathbf{Z})$ ”.

- p. 44, l. 2. Change “ $P$ ” to “ $P_\theta$ ”.
- p. 44, l. -13. “keep” should be “keep”.
- p. 46, l. 3. “ $\mu$ ” should be “ $\theta$ ” in the equation.
- p. 46, l. 8. “same risk as  $\delta^*(\mathbf{X})$ ” should be “same risk as  $\delta(\mathbf{X})$ ”.
- p. 47, l. -9. “The formula (1.5.8)” should be “The formula (1.2.8)”.
- p. 51, l. 9. natural sufficient statistics  $T^{(m)}(x) = \sum_{i=1}^m T(x_i)$ .
- p. 52, middle of page. “we show in Section 1.6.2” should be “we show in Theorem 1.6.3”.
- p. 53, l. 8. moment generating property
- p. 54, l. 1. “By Theorem 1.3.1” should be “By Theorem 1.5.1”.
- p. 54, l. 7. “ $\mathbf{T}^{(m)}(x)$ ” should be “ $\mathbf{T}^{(m)}(\mathbf{X})$ ”.
- p. 55, l.7. Should be : “ $\underline{T}(\underline{Y}) = (\sum Y_i, \sum z_i Y_i, \sum Y_i^2)^T$ ” (interchange  $T_2$  and  $T_3$ ).
- p. 55, l. 2. “ $\log(\pi / -\eta_2)$ ” should be “ $\log(\pi / (-\eta_2))$ ”.
- p. 57, l. -10. “ $\log(2\pi\lambda_0^2\theta^2)$ ” should be “ $\log(2\pi\lambda_0^{-2}\theta^2)$ ”.
- p. 58, l. 8. “ $\sum_{j=1}^n$ ” should be “ $\sum_{j=1}^3$ ”.
- p. 59, l. -11. “ $\eta_0, \eta_1 \in \varepsilon$ ” should be “ $\eta_1, \eta_2 \in \varepsilon$ ”.
- p. 59, Thm. 1.6.3. c) nonempty interior  $\mathcal{E}^0$  in  $R^k$  and  $\eta_0 \in \mathcal{E}^0$ .
- p. 60, l.60. Insert “ $n$ ” in front of the second, third, and fourth expression.
- p. 62, (1.6.16). “ $\pi^{-p/2}$ ” should be “ $(2\pi)^{-p/2}$ ”.
- p. 65, l. -12. “ $(T_1(X), \dots, T_k(X))$ ” should be “ $(T_1(X), \dots, T_k(X))^T$ ”.
- p. 66, formula for  $w$  in the middle of the page. Insert “ $t_{k+1}$ ” after “ $B(\underline{\theta})$ ”.
- p. 70, l. 2. “if the events  $T_1 \geq t, \dots, T_k \geq t$ ” should be “if and only if the events  $T_1 > t, \dots, T_k > t$ ”.
- p. 70, l. 10. “scale parameter  $\delta$ ” should be “scale parameter  $\delta^{-1}$ ”.
- p. 70, l. 14. “ $T_0$  and  $Y$ ” should be “ $T$  and  $Y$ ”.
- p. 78, l. 10.  $E(X - \mu)^4 = 3\sigma^4$ .
- p. 78, Prob. 1.3.8. (ii) “Let  $\hat{\sigma}_0^2 =$ ” should be “Let  $\hat{\sigma}_c^2 =$ ”.
- p. 80, l. -8. “predictor  $Y$ ” should be “predictor of  $Y$ ”.

- p. 81, l. -16. “ $Cor(Z, Y)$ ” should be “ $Corr(Z, Y)$ ”.
- p. 83, l. 13. “(2000)” should be “(2001)”.
- p. 84, **Problem 24(b)**. Should be “given  $Y = y$ ,  $Z \sim \mathcal{B}(n, y)$ ,  $n \geq 2$ ; and  $Y \sim \beta(r, s)$ . Find  $\mu_0(z)$  when (i)  $w(y, z) = 1$ , and (ii)  $w(y, z) = y(1 - y)$ ,  $0 < y < 1$ .”  
**Hint:** See Example 1.2.9.
- p. 86, l. 9.  $\frac{\partial}{\partial \theta} L_X(\theta)$  should be  $\frac{\partial}{\partial \theta} \log L_X(\theta)$ .
- p. 88, l. -14. parameter
- p. 89, l. -1. After “fixed time.” add “The lifetimes are assumed to be exponentially distributed.”.
- p. 90, **Hint to Prob. 1.6.16(ii)**. After “degrees of freedom,” insert “ $Y_0 = 0$ ”.
- p. 90, **Hint to Prob. 1.6.16(ii)**. “ $\sum_{i=1}^t Z_i$ ” should be “ $\sum_{i=1}^r Z_i$ ”.
- p. 90, **Prob. 1.6.17, l. 3**. “ $\mathbf{c}_{l \times 1}$ ” should be “ $\mathbf{c}_{k \times 1}$ ”.
- p. 90, l. 8. Should be “ $\pi_L$  is the projection matrix onto  $\mathcal{L} = \{\boldsymbol{\eta} : \boldsymbol{\eta} = B\boldsymbol{\theta}, \boldsymbol{\theta} \in R^l\}$ .”.
- p. 90, **Prob. 1.6.19, l. 6**. “ $\mathbf{z}_1, \dots, \mathbf{z}_d$ ” should be “the  $d$   $1 \times n$  rows of the matrix  $[\mathbf{z}_1, \dots, \mathbf{z}_d]_{d \times n}$ .”
- p. 91, **Prob. 27**. “genrated” should be “generated”.
- p. 91, **Prob. 1.6.28**. “information in theory” should be “information theory”.
- p. 91, **Prob. 28**. There needs to be  $dx$  in the last integration.
- p. 91, **Prob. 29, l. 3** “the  $p(p + 3)/2$  dimensional canonical exponential family.”
- p. 91, **Prob. 1.6.29**. “ $\mathbf{Y}_{ij}$ ” should be “ $Y_{ij}$ ”.
- p. 97, l. 6. “Statistics, 2000” should be “Statistics, 2001”.
- p. 99, **Formula (2.1.1)**. The gradient should be evaluated at the point  $\boldsymbol{\theta} = \boldsymbol{\theta}_0$ .
- p. 107, l. 3. “ $X \times H$ ” should be “ $X \times \Theta$ ”.
- p. 108, l. 8. Add the condition “ $\text{Var}(\epsilon_i) < \infty$ ”.
- p. 109, l. 16: “ $(\mathbf{z} - \mathbf{z}_0)$ ” should be “ $(z_j - z_{0j})$ ”
- p. 109, l. 17: “for  $\mathbf{z}_0$  an interior” should be “for  $\mathbf{z}_0 = (z_{01}, \dots, z_{0d})^T$  an interior”.
- p. 109, l. 17: “ $\frac{\partial \mu}{\partial z_j}(\mathbf{z}_0)\mathbf{z}_0$ ” should be “ $\frac{\partial \mu}{\partial z_j}(\mathbf{z}_0)z_{0j}$ ”.
- p. 113, **The expression for  $\hat{\beta}_1$  on the middle of the page**. Drop  $\frac{1}{n}$ 's (both of them).
- p. 113, l. -11. “Example 2.2.1” should be “Example 2.1.1”.

- p. 115, l. -9. and -8. Change “This estimate ...” to “Note that  $P(X_{(n)} = \theta) = 1 - P(\text{all } X_i < \theta) = 1 - [(\theta - 1)/\theta]^n \rightarrow 1 \text{ as } n \rightarrow \infty$ ”.
- p. 120, l. 16. After “model  $\mathcal{P}_0$ ” insert “(see (2.2.1))”.
- p. 124, l. 10. “ $\hat{\theta}_1 = \sqrt{n_1}/n$ ” should be “ $\hat{\theta}_1 = \sqrt{n_1/n}$ ”.
- p. 125, Formula (2.3.7). Formula is short one right parenthesis.
- p. 128, Thm. 2.4.1. ... “The interior of the convex support of  $p_T$ .” (Delete  $(a, b)$ .)  
*Proof.* After “ $f(b-)$ ” insert “if  $\mathcal{E} = (a, b)$ ”.
- p. 128. Step (3) of bisection algorithm should add “and return  $x_{\text{final}}$ ”.
- p. 130, Ex. 2.4.2. “ $\hat{b}_{\text{old}}$ ” should be “ $\hat{p}_{\text{old}}$ ”.
- p. 132, (2.4.3). There is one extra parenthesis at the end.
- p. 132, l. -3. “noncave” should be “non-concave”.
- p. 135, Lem. 2.4.1. “...and  $\theta_{\text{OLD}}$  maximizes  $J(\theta | \theta_{\text{OLD}})$ .”
- p. 137, Ex. 2.4.26. “ $\hat{\theta}_{\text{NEW}} = \frac{2N_{1m} + N_{2m}}{2n} + M_n / (2 - \hat{\theta}_{\text{OLD}})n$ .”
- p. 137, Eqn after (2.4.26).  $\theta^2 - \left(\frac{2+2N_{1m}+N_{2m}}{2n}\right)\theta + \frac{2N_{1m}+N_{2m}+M_n}{n} = 0$ .
- p. 137, l. 5. “Problem 2.4.12” should be “Problem 2.4.15”.
- p. 137, l. -5. Replace “and find (Problem 2.4.1)” with “It may be shown directly (Problem 2.4.1)...”.
- p. 138, l. 5-6. Delete the sentence beginning with “Because”.
- p. 141, Prob. 13(b)(iii). “Raleigh” should be “Rayleigh”.
- p. 143, Prob. 2.2.6(a). “ $E(Y_i) = \alpha z_j$  where the  $z_j$ ” should be “ $E(Y_i) = \alpha z_i$  where the  $z_i$ ”.
- p. 143, Prob. 2.2.7. “equations (2.1.5)” should be “equations (2.1.7)”.
- p. 151, l. -4. “ $h(z; \lambda)$ ” should be “ $h(z; \boldsymbol{\lambda})$ ”.
- p. 152, Prob. 2.3.4. “...of Corollary 2.3.1”.
- p. 153, l. 1. “heterogenous” should be “heteroscedastic”.
- p. 153, 8b). “ $\alpha = 1$  and  $p = 1$ .”
- p. 157, l. -3. “ $q(y, \theta_0)$ ” should be “ $q(s, \theta_0)$ ”.
- p. 158, l. 7. Replace “Limitations ... algorithm” with “*Limitations of the Missing Value Model of Example 2.4.6*”. The assumptions underlying Example 2.4.6...”.

- p. 158, 2.5.15. “Example 2.4.4”.
- p. 158, l. -17. Change “ $Y_i \leq 2$ ” to “ $Y_i \geq 2$ ”.
- p. 162, l. 3. Insert “minimum” before “Bayes risk”.
- p. 162, End of Paragraph 1. “Bayes procedure” should be “Bayes procedures”.
- p. 162, Beginning of Paragraph 3. “formulae (1.2.8)” should be “formula (1.2.8)”.
- p. 167, Ex. 3.2.4. “and  $\mu$  and the vector  $\Delta \dots$  is independent” should be “and  $\mu$  and the vector  $\Delta \dots$  are independent”.
- p. 169, l. 7. Insert “ $\sigma^{-2}$ ” in front of “ $\frac{1}{2}n(a - \theta)^2$ ”.
- p. 169, l. -2. “require” should be “requires”.
- p. 169, l. -18. “(2000)” should be “(2001)”.
- p. 170, l. 7. Possibly randomized *not* permitted.
- p. 170, l. 12.  $\bar{D} = \{\text{set of all randomized decision procedures}\}$ .
- p. 172, Top of Page. “ $R(\pi^{**}, \delta^{**})$ ” should be “ $r(\pi^{**}, \delta^{**})$ ”.
- p. 172, l. -5. In the integral of formula (3.3.13) replace “ $r(\theta, \delta)$ ” with “ $R(\theta, \delta)$ ”.
- p. 174, Thm. 3.3.3. In statement “.” after “prior distributions”, eliminate “such that  $\pi_k\{\theta : R(\theta, \delta^*) = r\} = 1$ , and”. Continue “Let ...”. First line in the proof should be “By assumption”.
- p. 175, l. 2 and 3. Replace “Then  $\dots = \sigma^2/n$ ” with “We know that  $R(\theta, \bar{X}) = \sigma^2/n$ ”.
- p. 182, Ex. 3.4.2. Strike “then”.
- p. 186, l. -7. Change “ $\log p(x, \theta)$ ” to “ $\log p(X, \theta)$ ”.
- p. 186, l. -6. Change “ $\sum \mathbf{Z}_Y^{-1}$ ” to “ $\sum \mathbf{Z}_Y^T$ ”.
- p. 190, Section 3.5.3. Missing period at end of paragraph 2.
- p. 194, l. 9 Should be “If  $[n\alpha] = [(n - 1)\alpha]$  and  $x^{([n\alpha])} = -x^{(n - [n\alpha])}$ ”.
- p. 195, l. 17 “ $(n^{-1}x)^2$ ” should be “ $(n - 1)(n^{-1}x)^2$ ”.
- p. 195, l.18 & 19: “ $\frac{1}{n^2}$ ” should be “ $\frac{n-1}{n^2}$ ”.
- p. 196, Remark 3.5.1. “ $\Delta_x(t) = 1[t \leq x]$ ” should be “ $\Delta_x(t) = 1[t \geq x]$ ”.
- p. 197, Pr. 4. After prior on  $\lambda$  add “and use squared error loss  $(\lambda - a)^2$ ”.
- p. 197, Pr. 5. (b)  $c$  should be  $c_w(x)$ , and  $c_w(x) = \int p(x|\theta)[\pi(\theta)/w(\theta)]d\theta$ .
- p. 198, Prob. 8, Hint for (a). “Cov( $\theta_j, \theta_j$ )” should be “Cov( $\theta_i, \theta_j$ )”.

- p. 201, **Prob. 3.3.7.** After “Show that” add “if”.
- p. 203, **Prob. 3.4.2.** “ $E(\delta(X) | t(X))$ ” should be “ $E(\delta(X) | T(X))$ ”.
- p. 203, **Prob. 3.4.5.** “ $\mu - \mu_0$ ” should be “ $\mu = \mu_0$ ”.
- p. 203, l. -1. After inadmissible add “under squared error loss”.
- p. 206, **Prob. 22:(ii).** Change “the information bound is infinite” to “ $I(\theta) = 1/\theta^2$ ”.
- p. 206, **Prob. 22:(iii).** Change “has finite variance” to “ $\text{Var}2x = 1/3\theta^2 < \theta^2$ ”.
- p. 212, l. 5,6. “mimimum” should be “minimum”. “2000” should be “2001”.
- p. 212, **3rd reference.** Insert “96, 746–774”.
- p. 214, l. 11.  $N_d = (N_{m1d}, N_{m0d}, N_{f1d}, N_{f0d})$  are independent with corresponding distributions  $\mathcal{M}(n_d, p_{m1d}, p_{m0d}, p_{f1d}, p_{f0d})$ ,  $1 \leq d \leq D$ .
- p. 216, l. 16. Insert “As we discussed in Section 1.3...” at the beginning of the sentence.
- p. 217, l. 10. Insert “As we have noted in Section 1.3” before “Such tests...”.
- p. 218, **Remark 4.1.** Replace “the level and size of the test” by “the size of the test”.
- p. 219, l. 15. “some equivalent” should be “some other”.
- p. 219, l. 18. Replace  $d\left(\frac{X}{n}, \theta_0\right)$  by  $d\left(\frac{X}{n}, [0, \theta_0]\right)$ .
- p. 222, l. -5, -6. “ $2n$ ” should be “ $2r$ ”.
- p. 224, l. -4. “is 0 or 1” should be “is 0 or in  $(0, 1]$ ”.
- p. 226, **Example 4.2.2, l. 4.** “ $(\mathbf{x} - \mu_1)$ ” should be “ $(\mathbf{x} - \boldsymbol{\mu}_1)$ ”. “ $(\mathbf{x} - \mu_0)$ ” should be “ $(\mathbf{x} - \boldsymbol{\mu}_0)$ ”.
- p. 226, l. -15. Shall read:  $Q = (\mathbf{X} - \boldsymbol{\mu}_0)^T \Sigma_0^{-1} (\mathbf{X} - \boldsymbol{\mu}_0) - (\mathbf{X} - \boldsymbol{\mu}_1)^T \Sigma_1^{-1} (\mathbf{X} - \boldsymbol{\mu}_1)$ .
- p. 228, l. 7. Change “ $P(N_1 \leq c)$ ” to “ $P(N_\ell \leq c)$ ”.
- p. 228, **Ex. 4.3.3.**  $\eta(\mu) = \sqrt{n}\mu/\sigma$ .
- p. 228, l. -1. “ $\theta > \theta_1$ ” should be “ $\theta > \theta_0$ ”.
- p. 229, l. 17. “most serious error” should be “more serious error”.
- p. 229, l. 20. “ $-\frac{1}{2}\log(2\pi\sigma^2)$ ” should be “ $-\frac{n}{2}\log(2\pi\sigma^2)$ ”.
- p. 229, **Ex. 4.3.5.** “test  $\delta^*$  with reject...” should be “test  $\delta^*$  which rejects...”.
- p. 232, **Paragraph before Ex. 4.3.7.** “invariance consideration” should be “invariance considerations”.
- p. 233, l. -9,-10. Delete the sentence beginning with “We also show that ” and replace

“Finally, we show” with “We also show”.

p. 234, **First equation at the top.**  $\geq$  should be  $\leq$ .

p. 235, **Second inequality at top.** “ $P[\bar{\nu}(X) = \nu]$ ” should be “ $P[\bar{\nu}(X) \geq \nu]$ ”.

p. 236, l. 22, 24, 25. (4.1.1) should be (4.4.1).

p. 236, l. 26. “larger than  $1 - \alpha$ ” should be “smaller than  $1 - \alpha$ ”.

p. 237, **Ex. 4.4.3.** The first equation should use  $\approx$ , not equality.

p. 237, l. 5. “ $s$ ” should be “ $s^2$ ”.

p. 238, l. -11. “ $n = \frac{k_\alpha}{l_0} - k_\alpha^2$ ” should be “ $n = \left(\frac{k_\alpha}{l_0}\right)^2 - k_\alpha^2$ ”.

p. 239, **Ex. 4.4.4.** “internet subscribers” should be “Internet subscribers”.

p. 239, l. -3. The pairs referred to should be “ $(\underline{q}_1, \bar{q}_1), \dots, (\underline{q}_r, \bar{q}_r)$ ”.

p. 240, **Ex. 4.4.5.** Change the two sentences at the end of this example to “The exact confidence coefficient is given in Problem 4.4.15.”

p. 241, **Ex. 4.4.7.** “case  $F$  supported...” should be “case of  $F$  supported...”. The right parenthesis after 1992 should actually be a comma, and a right parenthesis should come before the period at the end of the sentence.

p. 242, l. -12. At the right-hand side of the expression, “ $(1 - \alpha)$ ” should be “ $\alpha$ ”.

p. 243, l. -15. is a confidence interval .

p. 243, l. 10. Change “ $\nu_0 \in \mathcal{V}$ ” to “ $\nu_0 \in \mathcal{N}$ ”.

p. 243, **Proof of Thm. 4.5.1.** In the second equation, “ $s(t)$ ” should be “ $S(t)$ ”.

p. 244, **In the second line of Example 4.5.2.** Replace “Binomial” and “binomial” with “Bernoulli”.

p. 244, l. 11. “of a test  $\delta$ ” should be “of a level  $\alpha$  test  $\delta$ ”.

p. 244, l. 13. It should be  $\geq$  inside the  $C = \{ \}$ .

p. 244, l. -7. Replace “level  $(1 - \alpha)$  test” with “level  $\alpha$  test”.

p. 245, l. -8. “point o” should be “point of”.

p. 247, **Ex. 4.5.2.** In the second paragraph, the parameter of interest is mistakenly changed to “ $\theta$ ”.

p. 248, **Ex. 4.6.1.** Define  $k$  as the largest integer such that  $P(S \geq k) \geq (1 - \alpha)$ .

p. 248, **Formula (4.6.2).** The two  $\leq$ 's inside the brackets should both be  $\geq$ 's.

p. 249, l. 7: “Defined” should be “Define”.

- p. 249, l. -13. is a UMA .
- p. 251, In the second line of Definition 4.7.2. " $\pi(\cdot|x)$ " should be " $\pi(\theta|x)$ ".
- p. 252, Ex. 4.7.2, l. 8. Change " $(n-1)s^2$ " to " $t$ ".
- p. 252, Ex. 4.7.2, l. 9,10. Change " $(n-1)s^2/x_{n-1}(\alpha)$  of Example 4.4.2" to " $t/x_n(\alpha)$ ".
- p. 253, l. 10.  $E([\hat{Y} - \mu] + [Y - \mu])^2$  should read  $E([\hat{Y} - \mu] - [Y - \mu])^2$ .
- p. 253, l. -7. " $Z(Y)$ " should be " $Z_p(Y)$ ".
- p. 254, l. 6. "valid from samples..." should be "valid for samples...".
- p. 255, l. 10,15. " $\sigma_B^2$ " should be " $\hat{\sigma}_B^2$ ".
- p. 256, l. -14. " $\theta_0$  is of smaller" should be " $\Theta_0$  is of smaller".
- p. 258, l. 17. Reference should be: See Example 2.2.9.
- p. 259, One-third from top. "...is monotone increasing function..." should be "...is a monotone increasing function...".
- p. 261, l. -8. versus K .
- p. 264, l. -9. we are led to .
- p. 270, Prob. 4.1.6. There is no b). Delete a).
- p. 270, l. -12. Remove the word "complete".
- p. 271, Problem 9, l. 8. "the test that rejects  $H$  iff  $T \geq T_{(B+2-m)}$  has level  $m/(B+1)$ ".
- p. 271, Prob. 9. "Show that the test rejects  $H$ ..." should be "Show that the test that rejects  $H$ ...". "Next let  $T^{(1)}, \dots, T^{(B+1)}$ " should be "Next let  $T_{(1)}, \dots, T_{(B+1)}$ " and " $T \geq T^{(B+1-m)}$ " should be " $T \geq T_{(B+1-m)}$ ".
- p. 271, l. -1,-2. "Cramer" should be "Cramér".
- p. 274, Problem 3. " $\chi_{2n}^2$ " should be " $\chi_n^2$ ".
- p. 276, Problem 12. "Theorem 4.3.2" should be "Theorem 4.3.1".
- p. 278, Prob. 7, Hint. Reference to  $\bar{X}_{n_0}$  should be to the previously defined  $\bar{X}_0$ . Similarly,  $s_{n_0}$  should be  $s_0$ .
- p. 278, Problem 10(a). Should be "Show that this quadruple is sufficient".
- p. 279, Prob. 4.4.15. Change the whole problem into " (a) Show that the confidence coefficient of the rectangle of Example 4.4.5 is

$$\int_a^b \left[ 2\Phi\left(\sqrt{\frac{1}{n-1}}\sqrt{\tau} \cdot c\right) - 1 \right] g(\tau) d\tau$$



where  $a$  is the  $\frac{\alpha}{4}$ th quantile of the  $\chi_{n-1}^2$  distribution,  $b$  is the  $(1 - \frac{\alpha}{4})$ th quantile of the  $\chi_{n-1}^2$  distribution,  $c$  is the  $(1 - \frac{\alpha}{4})$ th quantile of the  $t$ -distribution, and  $g(\cdot)$  is the density function of the  $\chi_{n-1}^2$  distribution. (b) Compute the expression for  $\alpha = 0.05, 0.1$ , and compare them to  $1 - \alpha$ . Hint: Use Theorem B.3.3 and (B.1.30). Condition on  $[(n - 1)s^2/\sigma^2] = \tau$ ."

**p. 280, Prob. 4.4.18.** "Example 4.1.6" should be "Example 4.4.6".

**p. 284, l. 1 and 2.** Remove "100" from in front of " $x_{.95}$ " and " $x_{.05}$ ".

**p. 284, Pr. 13.** Let  $x_p = F^{-1}(p)$ ,  $0 < p < 1$ , be the 100 $p$ th quantile of  $F$ . And "100 $x_{.95}$ " should be " $x_{.95}$ ", "100 $x_{.05}$ " should be " $x_{.05}$ ".

**p. 284, Pr. 14.** "disstribution" to "distribution"

**p. 284, l. -1.** Insert " $= 1 - \alpha$ " on the right.

**p. 288, l. -1.** It should be " $\pi(t) = sc^s/t^{s+1}$ ,  $t > c$ ,  $s > 0$ ,  $c > 0$ ."

**p. 290, Problem 1(b).** "covers the true mean  $\mu$ " should be "covers  $X_{n+1}$ ".

**p. 290, l. 19.** " $X_i/\theta$ " should be " $2X_i/\theta$ ".

**p. 295, References.** Add the reference (see page 241): "Bickel, P. "Inference and auditing: the Stringer bound," Internat. Statist. Rev., 60, 197–209 (1992)."

**p. 296, l. 1,2.** Journal reference should be "Statistical Science", 101–128, 2001.

**p. 296, l. 5.** "Aarberge" should be "Aaberge".

**p. 297–298.** References to " $S$ " should be to " $s$ " (that's the usual notation).

**p. 299, l. -10.** Add after first sentence, "Without loss of generality, we assume  $\mu = 0$ ."

**p. 299, l. -3.** "Esseen" should be "Esséen".

**p. 300, Second paragraph from bottom.** "...results such as are..." should be "...results such as these are...".

**p. 302, Ex. 5.2.2.** " $\hat{P}$ " should be " $\hat{p}$ ".

**p. 302, Sentence after Ex. 5.2.2.** "suprising" should be "surprising".

**p. 304, l. -2.**  $\inf\{D(\theta_0, \theta) : |\theta - \theta_0| \geq \epsilon\} > D(\theta_0, \theta_0)$ .

**p. 305, formula (5.2.14)-(i).** " $|\rho(X_i, \theta) - D(\theta_0, \theta)|$ " should be " $[\rho(X_i, \theta) - D(\theta_0, \theta)]$ ".

**p. 305, l. 9.** " $|\theta - \theta_0| \geq \delta$ " should be " $|\theta - \theta_0| \geq \text{varepsilon}$ ".

**p. 306, "Summary".** "...sequence of estimates) consistency." should be "...sequence of estimates), consistency."

**p. 306, l. 11:** and derive consistency .

- p. 309, l. -4. Change “Problem 5.3.4” to “Problem 5.3.3”.
- p. 310, l. -9. Change “ $0(n^{-3})$ ” to “ $O(n^{-3})$ ”.
- p. 311, l. 10. Change “in (5.3.12)” to “in (5.3.13)”.
- p. 311, l. 11. After “(Problem 5.3.12)”, insert “, for  $d = 2$ ”.
- p. 313, l. -10. “Theorem 5.2.2” should be “Proposition 5.2.1”.
- p. 315, l. 5: and  $\sigma_1^2 = \sigma_2^2$ .
- p. 317, (5.3.19).  $\mathcal{L}_\gamma[\sqrt{n}(h(\hat{\gamma}_n) - h(\gamma))] \rightarrow \mathcal{N}(0, c)$
- p. 318, expression (5.3.20): “ $r_n^{(2)}$ ” should be “ $r_n$ ”.
- p. 318, l. 15: “ $E(V_n)^3$ ” should be “ $E(V - n)^3$ ”.
- p. 319, Example 5.3.6. In the third line, “ $\hat{\sigma}_X^2 \hat{\sigma}_Y^2$ ” should be “ $\hat{\sigma}_1^2 \hat{\sigma}_2^2$ ”. In the ninth line, “ $\frac{(x_i - \mu_1)}{\sigma}$ ” should be “ $\frac{(x_i - \mu_1)}{\sigma_1}$ ”.
- p. 320, l. 1. “ $\sigma_1^2, \sigma^2$ ” should be “ $\sigma_1^2, \sigma_2^2$ ”.
- p. 328, l. 9: “a parameter as defined in Section 1.1” should be “a well defined parameter as defined in Section 1.1.2”.
- p. 330, l. -13. After “are called  $M$ -estimates” insert “as well as estimating equation estimates — see Section 2.2.1”.
- p. 331, l. 13. “(5.4.20)” should be “(5.4.30)”.
- p. 331, First lines of Section 5.4.3 and Theorem 5.4.3. Insert minus sign in front of  $\ell(x, \theta)$  and  $\log p(x, \theta)$ .
- p. 334, l. 8. Drop footnote 3. At the end of the sentence, add “–see Problem 5.4.5”.
- p. 336, l. -2. Turning to method .
- p. 338, l. 15. It should read “denote the frequency of density function”.
- p. 344, l. -5. hypotheses specifying one point .
- p. 347, Problem 7: “Show that the maximum” should be “Show that the minimum”.
- p. 347, l.-7,-10. “maximum contrast estimate” should be “minimum contrast estimate”.
- p. 348, l. -1. Change “ $n^{-k/2}$ ” to “ $n^{-m/2}$ ”.
- p. 349, l. 1. Change “ $a_d \geq 0, 0 \leq j \leq m$ ” to “ $a_j \geq 0, 0 \leq j \leq d$ ”.
- p. 349, l. 2,3. Change “ $\sum_{j=1}^m$ ” to “ $\sum_{j=1}^d$ ”.

**p. 349, Problem 5.** Assume  $E|X_1|^j < \infty$ , change “ $i_1, \dots, i_j, j = 1, \dots, n$ ” to “ $1 \leq i_k \leq n, k = 1, \dots, n$ ” and change “ $E|X_1|$ ” to “ $E|X_1|^j$ ”.

**p. 350, 1.-9.** Should be  $\hat{X}_R = \bar{X} - b_{opt}(\bar{U} - \bar{u})$ .

**p. 350, 1.-5.** “ $X_1$ ” should be “ $X_i$ ”, and  $U_i$  are independent of  $\epsilon_i$ .

**p. 352, Problem 19(a).** Should be “ $h(\mu_1, \mu_2) + O(n^{-1})$ ”.

**p. 353, Pr. 23, 1. 4.** Change “ $\frac{1}{2}h^{(2)}(\mu) + \frac{\sigma^2}{n}$ ” to “ $\frac{1}{2}h^{(2)}(\mu)\sigma^2/n$ ”.

**p. 355, Pr. 30.** Change “Lemma 5.3.3” to “Lemma 5.3.1”. and “all integers  $k$ ” to “all integers  $k \geq 2$ ”. After “i.i.d. vectors” add “with zero means”.

**p. 355, Pr. 31(b):** “ $\chi_{n-1}$ ” should be “ $x_{n-1}$ ”.

**p. 356, 1. -3.** “ $f(\theta) = F'(\theta) > 0$  exists”.

**p. 358, 1. -1:** “(B.7.4)” should be “(B.7.5)”.

**p. 358, Problem 6:** This problem needs to be rewritten.

**6.** Show that for the likelihood ratio statistic

$$\log \Lambda_n = \sum_{i=1}^n \log \frac{p(X_i, \hat{\theta}_n)}{p(X_i, \theta_0)} 1(\hat{\theta}_n > \theta_0)$$

- **a)**  $\mathcal{L}_{\theta_0}(\log \Lambda_n) \rightarrow \mathcal{L}(U)$  where  $U \sim Z^2 1(Z > 0)$  where  $Z \sim \mathcal{N}(0, 1)$ .
- **b)**  $\mathcal{L}_{\theta_0 + \frac{\gamma}{\sqrt{n}}}(\log \Lambda_n) \rightarrow \mathcal{L} \left\{ \frac{1}{2} \left( Z + \gamma I^{\frac{1}{2}}(\theta_0) \right)^2 1 \left( Z > -\gamma I^{\frac{1}{2}}(\theta_0) \right) \right\}$ .
- **c)** Show that the level  $\alpha$  likelihood ratio test has asymptotic power function which achieves equality in (5.4.50).

**p. 360, Problem 1(a).** In the third line of 1(a), delete the “ $\tau$ ” before “ $(1 + n\tau^2)^{-1/2}$ ” and before “ $\bar{X}$ ”. After “Hint:” insert “Set  $T = \bar{X}$ . Then

$$\pi(\boldsymbol{\mu} = 0|t) = \lambda p(t|0)/p(t) \text{ where } p(t) = \lambda p(t|0) + (1 - \lambda) \int_{-\infty}^{\infty} \varphi_{\tau}(\mu) p(t|\mu) d\mu.$$

**p. 360, Problem 1(b).** Should be “Show that  $\tilde{\beta} \xrightarrow{P} 1$ ”.

**p. 361, Prob. 4.** “establish” should be “establish”.

**p. 368, 1. 15.** Should be “ $j = 1, \dots, p$ ”.

**p. 369, 1. 16 & 17.** “ $\mathcal{L}(\boldsymbol{\eta}, \mathbf{u})$ ” should be “ $l_{\mathbf{u}}(\boldsymbol{\eta})$ ”.

- p. 370, l. -10. Insert “,  $i = 1, \dots, r$ ” after “has  $\eta_i = U_i$ ”.
- p. 371, l. -13. Insert “If  $p = r$ , then” in front of “ $\hat{\beta}_j$  is the is the UMVU”.
- p. 373, l. 8. Replace “rank  $p$ ” with “full rank”.
- p. 373, l. -1. “ $\hat{\mu}$ ” should be “ $\hat{\alpha}$ ”.
- p. 373, Ex. 6.1.2, last line. Change “ $|\mathbf{Y} - \boldsymbol{\mu}|^2$ ” to “ $|\mathbf{Y} - \hat{\boldsymbol{\mu}}|^2$ ”.
- p. 374, l. -4: “ $H : 1 \leq q < r$ ” should be “ $0 \leq q \leq r$ ”.
- p. 375, l. 4: should be  $\lambda(Y) = \exp\{-\frac{1}{2\sigma^2}(|Y - \hat{\mu}|^2 - |Y - \hat{\mu}_0|^2)\}$ .
- p. 375, l. 10: Remove minus sign in fron of “ $-\frac{1}{2\sigma^2}$ ”.
- p. 375, l. -3. Change “Write  $\eta_i$ ” to “Write  $\boldsymbol{\eta}$ ”.
- p. 378, l. 10. Change “and  $\hat{\beta}_0$ ” to “and  $\hat{\beta}_1$ ”.
- p. 378, (6.1.27). Omit “ $(p - q)^{-1}$ ”.
- p. 379, l. 10: “(6.1.30)” should be “(6.1.29)”.
- p. 381, l. 5. Change “ $\mathbf{a}^T \boldsymbol{\mu}$ ” to “ $\mathbf{a}^T \hat{\boldsymbol{\mu}}$ ”.
- p. 381, l. 8. Change “ $(U_i/\sigma^2)$ ” to “ $(U_i/\sigma)$ ”.
- p. 383, l. -19.  $\sigma^2(\mathbf{Z}^T \mathbf{Z})^{-1}$ .
- p. 383, Ex. 6.1.2, Last line. Bold S
- p. 386, l. 2. Insert minus sign in front of  $\ell(x, \boldsymbol{\theta})$  and  $\log p(x, \boldsymbol{\theta})$ .
- p. 387, l. 10. After “minimum contrast” insert “or  $M$ ”.
- p. 389, l. 8. Change “ $(Z_{11}, \dots, Z_{1n})$ ” to “ $(Z_{11}, \dots, Z_{n1})$ ”, and “ $(Z_{j1}, \dots, Z_{jn})$ ” to “ $(Z_{1j}, \dots, Z_{nj})$ ”.
- p. 389, l. 11,12 etc. Change “ $Z_{21}, \dots, Z_{p1}$ ” to “ $Z_{12}, \dots, Z_{1p}$ ” and “ $Z_{j1}$ ” to “ $Z_{1j}$ ”.
- p. 390, (6.2.31).  $\int \boldsymbol{\Psi}(\mathbf{z}, y, \boldsymbol{\beta}, \sigma) dP$
- p. 390, l. -9. Change “ $c(f_0)$ ” to “ $c(f_0, \sigma)$ ” twice.
- p. 397, Theorem 6.3.3. The first two sentences should read “Suppose the assumptions of Theorem 6.3.2 and the previous conditions on  $\mathbf{g}$  hold. Suppose the MLE  $\hat{\boldsymbol{\theta}}_{0,n} \dots$ ”.
- p. 404, l. -5. In the summation, replace “ $N_i$ ” with “ $N_j$ ”.
- p. 415, l. -3. “ $Z_i^T$ ” should be “ $\mathbf{Z}_i^T$ ”.
- p. 416, l. 14: “(6.5.10)” should be “(6.5.12)”.
- p. 423, Pr. 7. Change “(6.1.28)” to “(6.1.27)”.

- p. 425, **Prob. 6.1.15(b)**. “ $x = 0.0289$ ” should be “ $s = 0.0289$ ”.
- p. 425, l. -1. “A5” should be “A6”.
- p. 426, **Pr. 5**. Change “ $c(f_0)$ ” to “ $c(f_0, \sigma)$ ”.
- p. 428, **Pr. 11, l. 3,4**. Change “ $Z_i^{(j)}$ ” to “ $Z_{ij}$ ” and “ $\sum_{j=1}^p$ ” to “ $\sum_{j=2}^p$ ”. Line 6, change “ $\beta_j$ ” to “ $\gamma_j$ ” and insert “where  $\gamma_j = \beta_j + c_j \beta_1$ ”.
- p. 429, l. -7. “ $k(\theta_0, \theta_1)$  is a Kullback–Leibler in formation” should be “ $K(\theta_0, \theta_1)$  is the Kullback–Leibler information”.
- p. 432, **Problem 4(b)**. “ $\theta_{12}/(\theta_{11} + \theta_{12})$ ” should be “ $\theta_{11}/(\theta_{11} + \theta_{12})$ ”.
- p. 434, **Problem 6.5.1**. “proosed” should be “proposed”.
- p. 436, **last line in Problem 436**. Change “then it is” to “then it does”.
- p. 442, l. -11. we can assign .
- p. 449, **(A.7.8)**: remove “= 1”.
- p. 451, **A.8.1**. It should read “ $X^{-1}(B)$  is in  $\mathcal{A} \dots$ ”.
- p. 452, l. -7.  $X$  has a marginal density .
- p. 454, l. 6. “ $1_A$ ” should be “ $1(A)$ ”.
- p. 454, l. 7. “ $1_A(\omega)$ ” should be “ $1(A)(\omega)$ ”.
- p. 455, l. 6: “If  $X = 1_A$ ” should be “If  $X = 1(A)$ ”.
- p. 458, l. -8 and -13. “Schwartz” should be “Schwarz”.
- p. 460, **expression (A.12.9)**: “ $c_\gamma$ ” should be “ $c_j$ ”.
- p. 463, l. 10. Insert “a” in front of “random variable”.
- p. 463, l. 16:  $F(X - \mu)$  should be  $F(x - \mu)$ .
- p. 464, **(A.13.17)**. “ $\sqrt{2\pi\sigma}$ ” should be “ $\sqrt{2\pi}\sigma$ ”.
- p. 465, l. 1. “ $e^{-\lambda}$ ” should be “ $e^{-\lambda x}$ ”.
- p. 467, **(A.14.13)**: extra right paren before first “(t)” .
- p. 470, **(A.15.10)**. Renumber as (A.15.11). Renumber unnumbered equation 7 lines above it as (A.15.10).
- p. 471. Renumber (A.15.11) as (A.15.12).
- p. 473. l. -10. and define .

- p. 473, l. -2. remove extra = .
- p. 478, (B.1.2). “ $p^y$ ” should be “ $p^z$ ”.
- p. 479, l. 4. “Bayes’ Rule” should be “Bayes’ theorem”.
- p. 479, (B.1.5) and below. “ $n - z$ ” should be “ $N - z$ ” and “ $\theta^y$ ” should be “ $\theta^z$ ”.
- p. 482, expression (B.1.22). “ $\binom{Z}{n}$ ” should be “ $\left(\frac{Z}{n}\right)$ ”.
- p. 482. l. -15.  $(1 - \theta)^{n-z}$  should be  $(1 - \theta)^{N-z}$ .
- p. 482. l. -9. Drop footnote 1.
- p. 482. l. -1. “Bayes’ Rule” should be “Bayes’ theorem”.
- p. 485. The last five lines should be italicized.
- p. 486, Thm. B.2.2. “ $\mathbf{Y} = g(\mathbf{Y})$ ” should be “ $\mathbf{Y} = g(\mathbf{X})$ ”.
- p. 487, l. 5: an example of the bivariate normal
- p. 491, l. -6. “ $(V/k)(W/m)$ ” should be “ $(V/k)/(W/m)$ ”.
- p. 492, (B.3.7). “ $S^{\frac{1}{2}(k-2)}$ ” should be “ $s^{\frac{1}{2}(k-2)}$ ”.
- p. 492. l. 12. Drop footnote 1.
- p. 495, (B.3.24). “ $N$ ” should be “ $n$ ”.
- p. 496, (B.3.26). “ $\sum_{j=1}^n a_{ij}$ ” should be “ $\sum_{j=1}^n a_{kj}$ ”.
- p. 498, l. 5. “ $\text{Cor}(X, Y)$ ” should be “ $\text{Corr}(X, Y)$ ”.
- p.502, l -15: “(Problem B.4.10)” should be “(Problem B.4.9)”.
- p.506, expression (B.5.19): “ $\Sigma$ ” should be bold.
- p. 507, l. 6: “(B.5.4)” should be “ (B.5.3)”.
- p. 507, (B.6.5). “ $|\det(\Sigma)|^{k/2}$ ” should be “ $|\det(\Sigma)|^{1/2}$ ”.
- p. 508, l. -5: “ $\mathbf{A}\Sigma\mathbf{A}'$ ” should be “ $\mathbf{A}\Sigma\mathbf{A}^T$ ”.
- p. 508, l. -3: “coordinates of  $\mathbf{D}$ ” should be “coordinates of  $\mathbf{U}$ ”.
- p. 509, (B.6.11): on the RHS the superscripts (1) in the denominator be (2).
- p. 509, Thm. B.6.5, last line. “ $\mu^{(1)-}$ ” should be “ $\mu^{(1)+}$ ”.
- p. 510, l. 6: “Theorem B.6.5” should be “Theorem B.6.4”.
- p. 512, 513, and 514. The subscript “ $n$ ” should not be bold.

**p. 514, Theorem B.7.5 Dominated Convergence Theorem.** It should be “If  $\{W_n\}$ ,  $W$  and  $V$  are random variables with  $W_n \xrightarrow{P} W$ ,  $P[|W_n| \leq |V|] = 1$  and  $E|V| < \infty$ , then  $EW_n \rightarrow EW$ .”

**p. 516:** the subscripts on “ $o$ ” and “ $O$ ” should be capital  $P$ .

**p. 518, l. 11.** “to strictly convex” should be “to be strictly convex”.

**p. 519, l. -5.** “The “if” part of (a)” should be “the “only if” part of (a)”.

**p. 525, Prob. B.1.8.** (iv) and (v) should read:

$$(iv) Y \sim \mathcal{U}(-1, 1), Z = Y^2$$

$$(v) Y \sim \mathcal{U}(-1, 1), Z = Y^2 \text{ if } Y^2 < \frac{1}{4} \text{ and } Z = \frac{1}{4} \text{ if } Y^2 \geq \frac{1}{4}$$

**p. 525, Prob. B.9(b).** “ $X$  and  $Y$  in Problem B.1.8(c)(i)” should be “ $Z$  and  $Y$  in Problem B.1.8(i)”.

**p. 526, l. 5.** Replace the hint by: Divide the numerator and denominator of the expression for  $P[Z = z | Y = y]$  on page 479 by  $\binom{N}{n} \binom{n}{y} \theta^y (1 - \theta)^{n-y}$ . This gives the required binomial probability in the numerator. Since the binomial probabilities add to one, the denominator must be one.

**p. 528, l. 8:**  $(X_{(1)}, \dots, X_{(n)})^T$  should be  $(X_{(1)}, \dots, X_{(r)})^T$ .

**p. 530, l. -4:** “ $\sum_{i=1}^{\infty}$ ” should be “ $\sum_{i=0}^{\infty}$ ”.

**p. 534, Prob. B.5.3.** “ $t_i^{i_1}$ ” should be “ $t_1^{i_1}$ ”.

**p. 534, l. -8:** The  $t$  in “ $K_U(t)$ ” should be bold.

**p. 535, l. 3:** “ $-2\sigma_{11}$ ” should be “ $-2\sigma_{11}^2$ ”.

**p. 535, l. -13.**  $i_{k_m}$  should be  $i_{k+m}$ .

**p. 535, Prob. B.6.3, last line.** “ $\Sigma_{22}$ ” should be “ $\Sigma_{22}^{-1}$ ”.

**p. 536, Problem 11.** “in Theorem B.7.6” should be “in Theorem B.7.7”.

**p. 543.** Label on the top figure should be  $Pr(Z \geq z)$ .

**p. 548, l. -16.** “Cauchy–Schwartz” should be “Cauchy–Schwarz”.

**p. 549, l. -13.** “Cramer” should be “Cramér”.

**p. 550, l. 12.** “Marakov” should be “Markov”.