# Statistics 2 <br> Second Midterm Exam <br> Fall 2002 

## Printed Name

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(Please also print your name at the top of each page)
Signature $\qquad$

## Student ID \#

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Circle the time of your section: $9: 00 \quad 10: 00 \quad 11: 00 \quad 12: 00 \quad 1: 00$

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | Total |
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There are 11 problems. A Normal table is at the end of the exam.
You can leave answers in unreduced form, for example as fractions, products, and factorials.

1. A fair coin is tossed three times.
a. [1] The chance that the third toss is heads equals $\qquad$ .
b. [1] The chance that the third toss is heads given that the first two tosses are tails equals $\qquad$ .
2. [2] A drawer contains three black socks and one red sock. Two socks are taken out in the dark. The chance that they are both black equals $\qquad$ .
3. [2] Five cards are dealt from a shuffled deck. The chance that at least one of them is a heart equals $\qquad$ .
4. One card is dealt from a shuffled deck. For each of the following, write in the blanks "mutually exclusive" if the two events are mutually exclusive, and "independent" if the two events are independent. If they are both mutually exclusive and independent, write "both," and if they are neither mutually exclusive nor independent write "neither."
a. [1] The card is an ace; the card is a heart.
b. [1] The card is a heart; the card is a diamond $\qquad$
5. Circle those of the following which can be calculated using the binomial probability formula:
a. [1] The chance that there are exactly three hearts among the first 20 cards dealt off the top of a shuffled deck.
b. [1] The chance that you toss a coin eight times until you get a total of three heads.
c. [1] The chance that a roulette wheel comes up black 12 times in 20 spins.
6. [2] A fair coin is tossed 100 times. The normal approximation is used to find approximately the chance of 50 or 51 heads. The result is the area under the normal curve between what two $z$-values (fill in the blanks)?
$\qquad$ \& $\qquad$
7. Lola tosses a fair coin 200 times and Manni tosses one 100 times. For each of the following, circle the more likely event.
a. [1] Lola gets 100 heads Manni gets 50 heads
b. [1] Lola gets between 95 and 105

Manni gets between 45 and 55
c. [1] Lola gets between 90 and 100 Manni gets between 45 and 55
8. Keno is a gambling game. If you bet a dollar on a single number and the number comes up you win, getting your dollar back plus $\$ 2$ (you win $\$ 2$ ). If you lose, you lose your dollar (you win $-\$ 1$ ). Your chance of winning is $25 \%$. Suppose you play Keno 100 times, betting $\$ 1$ on a single number each time. Fill in the blanks with the answers to each question:
a. [2] How much do you expect to win?
b. [2] What is the standard error of your total winnings?
c. [2] Approximately, what is the chance you come out ahead?
9. A city Housing Authority plans to survey households in rental units. (A household is defined as all the occupants of a single rental unit, for example, all the occupants of a single apartment). Indicate for each of the following whether the sample gathered as specified is a simple random sample of those households by circling "Yes" if it is and "No" if it is not.
a. [1] [Yes No] Within each zip code in the city, a list of rental households is assembled and 100 of them are chosen at random without replacement. The resulting sample consists of all the rental households chosen in this way from all the zip codes.
b. [1] [Yes No] A list of all buildings which contain rental units is compiled. $10 \%$ of them are chosen at random without replacement and then one rental unit from each of them is chosen at random.
c. [1] [Yes No] A list of all people living in rental units is assembled, 100 of them are chosen at random without replacement, and for each of those 100 , the household is selected to be in the sample.
10. The Housing Authority of the previous question planned to gather a simple random sample of 400 households out of a total of 20,000 . One of the questions they planned to ask was the rent paid during the previous month. From a survey the previous year, the investigators figured that the SD should be about $\$ 200$.
a. [2] True or False. If this guess at the population SD was correct, the error in using the sample average to estimate the population average would be $\$ 5$ or so.
b. [2] The sample average rent paid was $\$ 1100$ and the SD was $\$ 225$. A $90 \%$ confidence interval for the population average is
to $\qquad$ .
c. [1] True or False. About $90 \%$ of the rents in the city should fall within the interval above.
11. In October 2002, the Gallup Poll asked 1000 people whether they would support President Bush if he decided to invade Iraq. Assume for purposes of this question that this was a simple random sample of a population. The results are shown in the following figure. Consider estimating the percentage of the population who would not support the decision and do not think the U.S. should invade.
a. [2] Attach a standard error to the estimate of $22 \%$ :
b. [2] A $90 \%$ confidence interval for the population percentage is
$\qquad$ to $\qquad$ .


## Table



## A NORMAL TABLE

| $z$ | Height | Area | 2 | Height | Area | $z$ | Height | Area |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.00 | 39.89 | 0 | 1.50 | 12.95 | 86.64 | 3.00 | 0.443 | 99.730 |
| 0.05 | 39.84 | 3.99 | 1.55 | 12.00 | 87.89 | 3.05 | 0.381 | 99.771 |
| 0.10 | 39.69 | 7.97 | 1.60 | 11.09 | 89.04 | 3.10 | 0.327 | 99.806 |
| 0.15 | 39.45 | 11.92 | 1.65 | 10.23 | 90.11 | 3.15 | 0.279 | 99.837 |
| 0.20 | 39.10 | 15.85 | 1.70 | 9.40 | 91.09 | 3.20 | 0.238 | 99.863 |
| 0.25 | 38.67 | 19.74 | 1.75 | 8.63 | 91.99 | 3.25 | 0.203 | 99.885 |
| 0.30 | 38.14 | 23.58 | 1.80 | 7.90 | 92.81 | 3.30 | 0.172 | 99.903 |
| 0.35 | 37.52 | 27.37 | 1.85 | 7.21 | 93.57 | 3.35 | 0.146 | 99.919 |
| 0.40 | 36.83 | 31.08 | 1.90 | 6.56 | 94.26 | 3.40 | 0.123 | 99.933 |
| 0.45 | 36.05 | 34.73 | 1.95 | 5.96 | 94.88 | 3.45 | 0.104 | 99.944 |
| 0.50 | 35.21 | 38.29 | 2.00 | 5.40 | 95.45 | 3.50 | 0.087 | 99.953 |
| 0.55 | 34.29 | 41.77 | 2.05 | 4.88 | 95.96 | 3.55 | 0.073 | 99.961 |
| 0.60 | 33.32 | 45.15 | 2.10 | 4.40 | 96.43 | 3.60 | 0.061 | 99.968 |
| 0.65 | 32.30 | 48.43 | 2.15 | 3.96 | 96.84 | 3.65 | 0.051 | 99.974 |
| 0.70 | 31.23 | 51.61 | 2.20 | 3.55 | 97.22 | 3.70 | 0.042 | 99.978 |
| 0.75 | 30.11 | 54.67 | 2.25 | 3.17 | 97.56 | 3.75 | 0.035 | 99.982 |
| 0.80 | 28.97 | 57.63 | 2.30 | 2.83 | 97.86 | 3.80 | 0.029 | 99.986 |
| 0.85 | 27.80 | 60.47 | 2.35 | 2.52 | 98.12 | 3.85 | 0.024 | 99.988 |
| 0.90 | 26.61 | 63.19 | 2.40 | 2.24 | 98.36 | 3.90 | 0.020 | 99.990 |
| 0.95 | 25.41 | 65.79 | 2.45 | 1.98 | 98.57 | 3.95 | 0.016 | 99.992 |
| 1.00 | 24.20 | 68.27 | 2.50 | 1.75 | 98.76 | 4.00 | 0.013 | 99.9937 |
| 1.05 | 22.99 | 70.63 | 2.55 | 1.54 | 98.92 | 4.05 | 0.011 | 99.9949 |
| 1.10 | 21.79 | 72.87 | 2.60 | 1.36 | 99.07 | 4.10 | 0.009 | 99.9959 |
| 1.15 | 20.59 | 74.99 | 2.65 | 1.19 | 99.20 | 4.15 | 0.007 | 99.9967 |
| 1.20 | 19.42 | 76.99 | 2.70 | 1.04 | 99.31 | 4.20 | 0.006 | 99.9973 |
| 1.25 | 18.26 | 78.87 | 2.75 | 0.91 | 99.40 | 4.25 | 0.005 | 99.9979 |
| 1.30 | 17.14 | 80.64 | 2.80 | 0.79 | 99.49 | 4.30 | 0.004 | 99.9983 |
| 1.35 | 16.04 | 82.30 | 2.85 | 0.69 | 99.56 | 4.35 | 0.003 | 99.9986 |
| 1.40 | 14.97 | 83.85 | 2.90 | 0.60 | 99.63 | 4.40 | 0.002 | 99.9989 |
| 1.45 | 13.94 | 85.29 | 2.95 | 0.51 | 99.68 | 4.45 | 0.002 | 99.9991 |

